

Visual segmentation by contextual influences via intra-cortical interactions in the primary visual cortex

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Abstract. Stimuli outside classical receptive fields have been shown to exert a significant influence over the activities of neurons in the primary visual cortex. We propose that contextual influences are used for pre-attentive visual segmentation. The difference between contextual influences near and far from region boundaries makes neural activities near region boundaries higher than elsewhere, making boundaries more salient for perceptual pop-out. The cortex thus computes *global* region boundaries by detecting the breakdown of homogeneity or translation invariance in the input, using *local* intra-cortical interactions mediated by the horizontal connections. This proposal is implemented in a biologically based model of V1, and demonstrated using examples of texture segmentation and figure-ground segregation. The model is also the first that performs texture or region segmentation in exactly the same neural circuit that solves the dual problem of the enhancement of contours, as is suggested by experimental observations. The computational framework in this model is simpler than previous approaches, making it implementable by V1 mechanisms, though higher-level visual mechanisms are needed to refine its output. However, it easily handles a class of segmentation problems that are known to be tricky. Its behaviour is compared with psycho-physical and physiological data on segmentation, contour enhancement, contextual influences and other phenomena such as asymmetry in visual search.

1. Introduction

In early stages of the visual system, individual neurons respond directly only to stimuli in their classical receptive fields (RFs) (Hubel and Wiesel 1962). These RFs sample the *local* contrast information in the input, but are too small to cover visual objects at a *global* scale. Recent experiments show that the responses of primary cortical (V1) cells are significantly influenced by stimuli nearby and beyond their classical RFs (Allman *et al* 1985, Knierim and van Essen 1992, Gilbert 1992, Kapadia *et al* 1995, Sillito *et al* 1995, Lamme 1995, Zipser *et al* 1996, Levitt and Lund 1997). These contextual influences are, in general, suppressive and depend on whether stimuli within and beyond the RFs share the same orientation (Allman *et al* 1985, Knierim and van Essen 1992, Sillito *et al* 1995, Levitt and Lund 1997). In particular, the response to an optimal bar in the RF is suppressed significantly by similarly oriented bars in the surround—iso-orientation suppression (Knierim and van Essen 1992). The suppression is reduced when the orientations of the surround bars are random or different from the bar in the RF (Knierim and van Essen 1992, Sillito *et al* 1995). However, if the surround bars are aligned with the optimal bar inside the RF to form a smooth contour, then suppression becomes facilitation (Kapadia *et al* 1995). The contextual influences are apparent within 10–20 ms after the cell's initial response (Knierim and van Essen 1992, Kapadia *et al* 1995),

suggesting that mechanisms within V1 itself are responsible (see the discussion later on the different time scales observed by Zipser *et al* (1996)). Horizontal intra-cortical connections linking cells with non-overlapping RFs and similar orientation preferences have been observed and hypothesized as the underlying neural substrate (Gilbert and Wiesel 1983, Rockland and Lund 1983, Gilbert 1992).

There have been some models on the underlying neural circuits (e.g. Somers *et al* 1995, Stemmler *et al* 1995) to explain the orientation- and contrast-dependent contextual influences observed physiologically. In terms of visual computation, the insight into the roles of the contextual influences is mainly limited to contour or feature linking (Allman *et al* 1985, Grossberg and Mingolla 1985, Gilbert 1992, see the discussions later and more references in Li 1998a). In a previous publication (Li 1998b), we studied how the contextual influences can indeed selectively enhance neural responses to segments of smooth contours against a noisy background. In this paper, we will show that the contextual influences serve a much more extensive computational goal of pre-attentive segmentation by enhancing neural responses to important image locations such as borders between texture regions and small figures against backgrounds, and that enhancing the contour segments is only a particular case of such a computation. The enhanced neural responses to these important image locations make them more salient, maybe even pop out, for further processing or to attract visual attention, thus serving pre-attentive segmentation. This is a computation on a *global* scale, such as on the texture regions and contours (which may represent boundaries of underlying objects) in an image, using *local* classical RF features and *local* intra-cortical interactions within a few RF sizes. Note that although the horizontal intra-cortical connections are termed long range in the literature, they are still local with respect to the whole visual field since the axons reach only a few millimetres (Gilbert 1992), or a few hypercolumns or receptive field sizes, away from the pre-synaptic cells. Although the primary visual cortex is a low-level visual area, we show below how it can play an important role in segmentation. In this paper, while we present the general framework of pre-attentive segmentation by V1 mechanisms using a model, the behaviour of the model is demonstrated mostly by examples of region segmentation and figure-ground segregation. Most details on the particular aspect of the computation—contour enhancement—can be found in a previous publication (Li 1998b).

2. The problem of visual segmentation

Visual segmentation is defined as locating the boundary between different image regions. There are two classes of approaches to segmentation—edge/contour based and region based (Kasturi and Jain 1991, Haralick and Shapiro 1992). For example, when regions are defined by their pixel luminance values, one can either use an edge-based approach to locate boundaries by finding (and linking) the edge or luminance contrast, which is large at the region boundaries, or use region-based approaches by comparing the luminance or the feature classification values between neighbouring image areas to find where features change. In general, regions are seldom classifiable by pixel luminances. Distracting luminance edges are often abundant within texture regions whose borders often do not correspond to any definite luminance edges or contour, making edge-based approaches difficult. Although most edge-based algorithms define edges as contrast in luminance, one may also use edges defined by contrasts in other features such as texture or motion; the resulting algorithm for edge or boundary finding requires classifying the region (e.g. texture or motion) features first (Kasturi and Jain 1991) and is then essentially a region-based approach as described

below. For region-based segmentation on general images, segmentation requires implicitly or explicitly:

- (a) for every small image area, to extract and classify image feature (such as image statistics by pixel correlations, or the model parameters in the Markov random fields generating the image (Haralick and Shapiro 1992), or the outcomes from model neural filters (Bergen and Adelson 1988) or model neural interactions (Malik and Perona 1990));
- (b) comparisons of the classification flags (feature values) between neighbouring image areas to locate the boundary as where the classification flags change.

In such approaches, classification is problematic and ambiguous near region boundaries where different features from different regions contribute to the feature estimate for an image area. One may also combine region- and edge-based approaches (Kasturi and Jain 1991). However, the outcomes of the two approaches often conflict with each other and combining them is seldom easy.

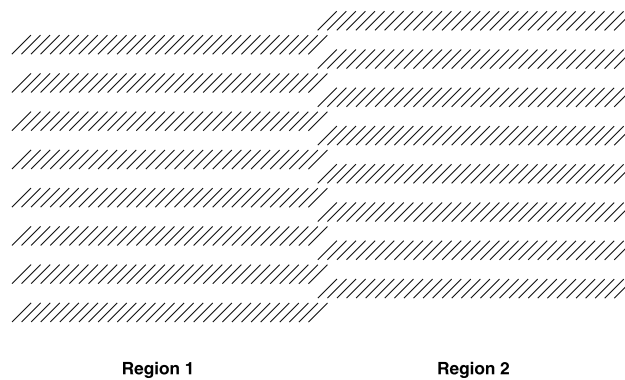


Figure 1. The two regions have the same feature values, and there are no vertical contrast edges at the vertical region border. Traditional approaches using region- or edge/contour-based approaches have difficulty in segmenting the regions.

Natural vision can easily segment the two regions in figure 1. However, this example is difficult for computer vision algorithms to segment whether one uses edge- or region-based algorithms. While edge-based segmentation algorithms would not identify any vertical luminance edges corresponding to the true boundary but many distracting edges within each region, region-based algorithms would find the same texture feature in both regions and thus no feature contrasts to locate the boundary. We propose that pre-attentive visual mechanisms in V1 locate the region boundaries by locating where homogeneities in inputs break down, and highlight such locations by higher neural responses. In principle, such a V1 algorithm corresponds to an edge/boundary-based approach in computer vision. However, it is more general than most boundary-based algorithms because the mechanism is not restricted to contrast in luminance or any particular feature such as texture, as long as input homogeneity is broken. Furthermore, as we will show below, the V1 mechanism locates the boundary without explicit feature classification and comparison between neighbouring image areas, thereby avoiding the difficulty forced by region-based approaches in the example of figure 1. In this sense, our proposed segmentation in V1 can be seen as *segmentation without classification*, in contrast with traditional approaches. This pre-attentive segmentation is in some sense the bare minimum component of segmentation, and is of low level and primitive such that not

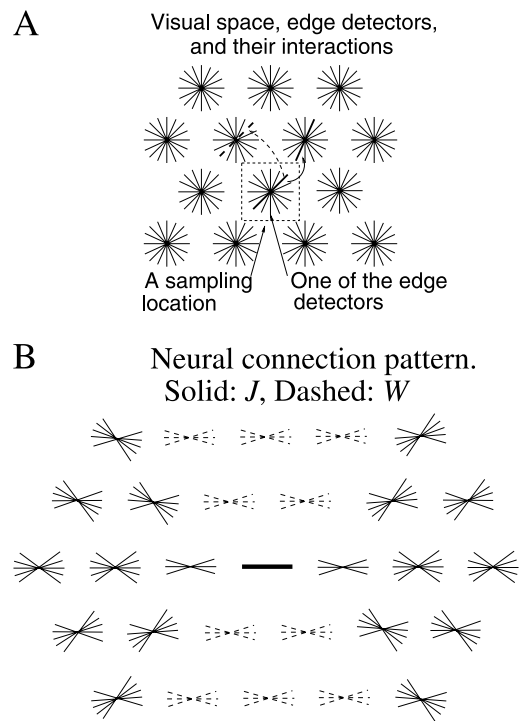
all regions can be segmented from others, just as humans cannot pre-attentively segment, for example, an area of 'T's from an area of 'L's. This also means that higher visual areas are needed to improve and refine the segmentation outcomes from V1. However, the pre-attentive mechanism in V1 is of general purpose enough that it can handle contour enhancement (a special case of boundary-based segmentation), texture boundary location (highlight) and the pop-out of figures against a background within the same neural circuit, as will be shown below.

3. The principle and its model implementation

The basic computational principle is to detect region boundaries by detecting the breakdown of translation invariance in inputs. A single image region is assumed to be defined by the homogeneity or translation invariance of the statistics of the image features, no matter what the features are, for instance, whether they are coloured red or blue or whether or not the texture elements are textons (Julesz 1981). In general, this translation invariance should include cases such as the image of a surface slanted in depth, although the current implementation of the principle has not yet been generalized beyond images of fronto-parallel surfaces. Homogeneity is disrupted or broken at the boundary of a region. In pre-attentive segmentation, a mechanism signals the location of this disruption without explicitly extracting and comparing the features in image areas.

This principle is implemented in a model of V1. Without loss of generality, the model focuses on texture segmentation, i.e. segmentation without colour, motion, luminance or stereo cues. To focus on the segmentation problem, the model includes mainly layer 2–3 orientation-selective cells and ignores the mechanism by which their receptive fields are formed. Inputs to the model are images filtered by the edge- or bar-like local RFs of V1 cells. (The terms 'edge' and 'bar' will be used interchangeably.) The resulting bar inputs are merely image primitives, which are in principle like image pixel primitives and are reversibly convertible from them†. They are *not* texture feature values, such as the '+' or '×' patterns in figure 5(E) and the statistics of their spatial arrangements, or the estimated densities of bars of particular orientations, from which one cannot recover the original input images. To avoid confusion, the rest of the paper uses the term 'edge' only for local luminance contrast, a boundary of a region is termed 'boundary' or 'border' which may or may not (especially for texture regions) correspond to any 'edges' in the image. The cells influence each other contextually via horizontal intra-cortical connections (Rockland and Lund 1983, Gilbert and Wiesel 1983, Gilbert 1992), transforming patterns of inputs to patterns of cell responses. If cortical interactions are translation invariant and do not induce spontaneous pattern formation (such as zebra stripes (Meinhardt 1982)) through the spontaneous breakdown of translation symmetry, then the cortical response to a homogeneous region will itself be homogeneous. However, if there is a region boundary, then two neurons, one near and another far from the boundary, will experience different contextual influences, and thus respond differently. In the model, the cortical interactions are designed (see below) such that the activities of neurons near the boundaries will be relatively higher. This makes the boundaries relatively more salient, allowing them to pop out perceptually for pre-attentive segmentation. Experiments in V1 indeed show that activity levels are robustly higher near simple texture boundaries only 10–15 ms after the initial cell responses (Nothdurft 1994, Gallant *et al* 1995).

† In practice, in the presence of noise, it is not possible to uniquely reconstruct the original pixel values in the input image from the 'edge' and 'bar' variables. For simplicity, the current implementation has not enforced this reversibility. However, the principle of no classification is adhered to by not explicitly comparing (whether by differentiation or other related techniques) the 'edge' and 'bar' values between image areas to find region boundaries.



C Model Neural Elements



Figure 2 shows the elements of the model and their interactions. At each location i there is a model V1 hypercolumn composed of K neuron pairs. Each pair (i, θ) has RF centre i and preferred orientation $\theta = k\pi/K$ for $k = 1, 2, \dots, K$, and is called (a neural representation of) an edge segment. Based on experimental data (White 1989, Douglas and Martin 1990), each edge segment consists of an excitatory and an inhibitory neuron that are connected with each other. Each model cell represents a collection of local cells of similar types, hence a 1:1 ratio of the number of model excitatory cells and inhibitory cells does not imply that there is a 1:1 ratio in the real cortex, for which the ratio is actually larger than 1. The excitatory cell receives the visual input; its output quantifies the response or salience of the edge segment and projects to higher visual areas. The inhibitory cells are treated as interneurons. An edge of input strength $I_{i\beta}$ at i with orientation β in the input image contributes to $I_{i\theta}$ by an amount $\hat{I}_{i\beta}\phi(\theta - \beta)$, where $\phi(\theta - \beta) = e^{-|\theta - \beta|/(\pi/8)}$ is the cell's orientation tuning curve. Based on observations by Gilbert, Lund and their colleagues (Gilbert and Wiesel 1983, Rockland and Lund 1983, Hirsch and Gilbert 1991), horizontal connections $J_{i\theta, j\theta'}$ (respectively, $W_{i\theta, j\theta'}$) mediate contextual influences via monosynaptic excitation (respectively, disynaptic inhibition) from bar $j\theta'$ to $i\theta$ which have nearby but different RF centres, $i \neq j$, and similar orientation preferences, $\theta \sim \theta'$. The membrane potentials follow the equations:

$$\begin{aligned} \dot{x}_{i\theta} = & -\alpha_x x_{i\theta} - g_y(y_{i,\theta}) - \sum_{\Delta\theta \neq 0} \psi(\Delta\theta) g_y(y_{i,\theta+\Delta\theta}) + J_o g_x(x_{i\theta}) \\ & + \sum_{j \neq i, \theta'} J_{i\theta, j\theta'} g_x(x_{j\theta'}) + I_{i\theta} + I_o \end{aligned} \quad (1)$$

$$\dot{y}_{i\theta} = -\alpha_y y_{i\theta} + g_x(x_{i\theta}) + \sum_{j \neq i, \theta'} W_{i\theta, j\theta'} g_x(x_{j\theta'}) + I_c \quad (2)$$

where $\alpha_x x_{i\theta}$ and $\alpha_y y_{i\theta}$ model the decay to the resting potential, $g_x(x)$ and $g_y(y)$ are sigmoid-like functions modelling cells' firing rates in response to membrane potentials x and y , respectively, $\psi(\Delta\theta) \leq 1$ is the spread of inhibition within a hypercolumn, $J_o g_x(x_{i\theta})$ is self-excitation, I_c and I_o are background inputs, including noise and inputs modelling the general and local normalization of activities (Heeger 1992) (see the appendix for more details). Visual input $I_{i\theta}$ persists after onset, and initializes the activity levels $g_x(x_{i\theta})$. Equations (1) and (2) specify how the activities are then modified (effectively within one membrane time constant) by the contextual influences. Depending on the visual stimuli, the system often settles into an oscillatory state (Gray and Singer 1989, Eckhorn *et al* 1988), a common intrinsic property of a population of recurrently connected excitatory and inhibitory cells. Temporal averages of $g_x(x_{i\theta})$ over several oscillation cycles (about 12–24 membrane time constants) are used as the model's output. If the maxima over time of the responses of the cells were used instead as the model's output, the boundary effects shown in this paper would usually be stronger. That different regions occupy different oscillation phases could be exploited for segmentation (Li 1998b), although we do not do so here. The nature of the computation performed by the model is determined largely by the horizontal connections J and W .

For view-point invariance, the connections are local, and translation and rotation invariant (figure 2(B)), i.e. every pyramidal cell has the same horizontal connection pattern in its egocentric reference frame. The synaptic weights are designed for the segmentation task, while staying consistent with experimental observations (Rockland and Lund 1983, Gilbert and Wiesel 1983, Hirsch and Gilbert 1991, Weliky *et al* 1995). In particular, J and W are chosen to satisfy the following three conditions (Li 1998a):

- (1) the system should not generate patterns spontaneously, i.e. homogeneous input images should give homogeneous outputs, so that no illusory borders will be formed within a single region;

- (2) neurons at region borders should give relatively higher responses; and
- (3) the same neural circuit should perform contour enhancement.

Condition (3) is not only required by physiological facts (Knierim and van Essen 1992, Kapadia *et al* 1995), but is also desirable because regions and their boundary contours are complementary. The qualitative structure of the connection pattern satisfying the conditions resembles a ‘bow tie’: J predominantly links cells with aligned RFs for contour enhancement, and W predominantly links cells with non-aligned RFs for surround suppression (figure 2(B)). Both J and W link cells with similar orientation preferences, as observed experimentally (Rockland and Lund 1983, Gilbert and Wiesel 1983, Hirsch and Gilbert 1991, Weliky *et al* 1995). Since this qualitative connection pattern is derived from the three conditions given above, it is thus a prediction of our computational requirements. The connection strength between cells decays with distance between the RFs, and is zero between cells separated by long distances (see the appendix). Once the choice of the connection strengths is set by the three conditions, they are not varied in the application of our model to any visual input patterns. This is because, by our computational design, varying the connections beyond the bound of the three conditions will inevitably destroy the computational properties of the model. For instance, if the connections are changed such that condition (1) is no longer met, then the model will produce output highlights at image locations where there should be none, and these hallucinated highlights would compete with and even overwhelm the highlights generated by the actual region borders or pop-out targets at other locations in the image.

Mean field techniques and dynamic stability analysis (shown in the appendix) are used to design the horizontal connections that ensure the three conditions. Conditions (1) and (2) are strictly met only for (the particularly homogeneous) inputs $I_{i\theta}$ within a region that are independent of i , i.e. exactly the same inputs are received at each grid point. When a region receives more complex input texture patterns such as in stochastic or sparse texture regions (e.g. those in figure 5), conditions (1) and (2) are often met but not guaranteed. This is not necessarily a flaw in this model, since it is not clear whether conditions (1) and (2) can always be met for any type of homogeneous inputs within a region under the hardware constraints of the model or the cortex. This is consistent with the observations that sometimes a texture region does not pop out of a background pre-attentively in human vision (Bergen 1991). A range of quantitatively different connection patterns can meet the three restrictive conditions. Of course, this range depends on the particular structure and parameters of the model such as its receptive field sampling density. This makes the model quantitatively imprecise compared to physiological and psycho-physical observations (see discussions later). The quantitative model parameters used for horizontal connections and neural elements to reproduce all our results are also listed in the appendix.

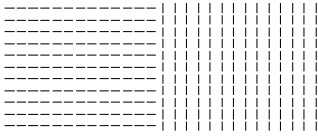
4. Performance of the model

Figures 3–10 show the results of applying the model to a variety of input patterns. With a few exceptions, the input value $\hat{I}_{i\theta}$ is the same for all visible bars in each example so that any differences in the responses $g_x(x_{i\theta})$ to the bars are solely due to the effects of the intra-cortical interactions. The exceptions are the input taken from a photograph (figure 10), an input in figure 9(C) to test the robustness of texture segmentation to random input strength variations, and the input in figure 8(D), which models an experiment on contour enhancement (Kapadia *et al* 1995). The differences in the outputs, which are interpreted as differences in saliencies, are significant about one membrane time constant after the initial neural response. This agrees with experimental observations (Knierim and van Essen 1992, Kapadia *et al* 1995, Gallant

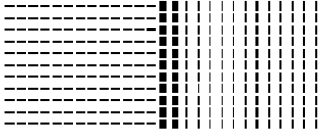
et al 1995) if this time constant is assumed to be of the order of 10 ms. The actual value $\hat{I}_{i\theta}$ used in all examples is chosen to mimic the corresponding experimental conditions. In this model the dynamic range is $\hat{I}_{i\theta} = (1.0, 4.0)$ for an isolated bar to drive the excitatory neuron from threshold activation to saturation. Hence, we use $\hat{I}_{i\theta} = 1.2, 2.0$ and 3.5 for low-, intermediate- and high-contrast input conditions used in experiments. Low input levels are used to demonstrate contour enhancement—the visible bars in figure 6(C) and the target bar in figure 8(D) (Kapadia *et al* 1995, Polat and Sagi 1993, Field *et al* 1993, Kovacs and Julesz 1993). Intermediate or high levels are used for all visible bars in texture segmentation and figure-ground pop-out examples (figures 3–5, 6(A, B), 7 and 9). High input levels are used for all visible bars in figures 8(A–C) and the contextual (background) bars in figure 8(D) to model the high-contrast conditions used in physiological experiments that study contextual influence from textured and/or contour backgrounds (Knierim and van Essen 1992, Kapadia *et al* 1995). The input $I_{i\theta}$ from a photographic image (figure 10) is different for different $i\theta$ with $I_{i\theta} \leq 3.0$. The output saliency $g_x(x_{i\theta})$ ranges between 0 and 1. The widths of the bars in the figures are proportional to input or output strengths. The same model parameters (e.g. the dependence of the synaptic weights on distances and orientations, the thresholds and gains in the functions $g_x(\cdot)$ and $g_y(\cdot)$, and the level of input noises in I_o) are used for all the examples whether it is for the texture segmentation, contour enhancement, figure-ground segregation, or combinations of them. The only differences between different examples are the differences in the model inputs $I_{i\theta}$ and possibly the different image grid structure (Manhattan or hexagonal grids) for better input sampling. We visualize the most salient outputs in some figures by plotting the bars that induce response levels higher than some threshold. V1, of course, does not threshold its outputs, we use the threshold only for display purposes. It is possible that higher visual centres could attend to a selected portion of the input by such thresholds, with an increasing value of the threshold for decreasing areas of the attended input.

Figure 3(A) shows a sample input containing two regions. Figure 3(B) shows the model output. Note that the plotted region is only a small part of, and extends continuously to, a larger image. This is the case for all figures in this paper except figure 10. Figure 3(C) plots the saliency $S(c)$ averaged over the bars in each column c in figure 3(B), indicating that the most salient bars are indeed near the region boundary. Figure 3(D) confirms that the boundary can be identified by thresholding the output activities using a threshold, denoted as, say, $thre = 0.5$ in figure 3(D), the fraction of the highest output $\max_{i\theta} \{g_x(x_{i\theta})\}$ in the image. To quantify the relative saliency of the boundary, define the net saliency at each grid point i to be that of the most activated bar ($\max_{\theta} \{g_x(x_{i\theta})\}$), let S_{peak} be the average saliency across the most salient grid column parallel and near the boundary, and $\bar{S}$ and σ_s be the mean and standard deviation in the saliencies of all locations including the boundary. Define ($r \equiv S_{\text{peak}}/\bar{S}$, $z \equiv (S_{\text{peak}} - \bar{S})/\sigma_s$). A salient boundary should give large values (r, z). One expects that at least one of r and z should be comfortably larger than 1 for the boundaries to be adequately salient. In figure 3, (r, z) = (3.7, 4.0). Note that the vertical bars near the boundary are more salient than the horizontal ones. This is because the vertical bars run parallel to the boundary, and are therefore specially enhanced through the contour enhancement effect of the contextual influences. This is related to the psycho-physical observation that texture boundaries are stronger when the texture elements on one side of them are parallel to the boundaries (Wolfson and Landy 1994). Figure 4(A) shows an example with the same orientation contrast (90°) at the boundary as in figure 3, but for different orientations of the texture bars. Here the saliency values distribute symmetrically across the boundary and the boundary strength is a little weaker. Figures 3 and 4(A) together predict that the neural response near a texture border is tuned to the border orientation relative to the optimal orientation of the bar within the RF, given an orientation contrast at the border, and that the optimal orientation of the border is the same as that of the bar within the RF.

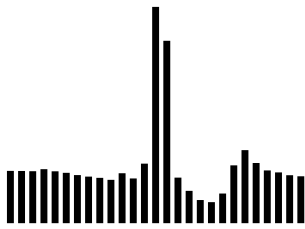
A: Input image ($I_{i\theta}$) to model



B: Model output



C: Neural response levels
vs. columns above



D: Thresholded model output



Figure 3. An example of the segmentation performance of the model. (A) Input $\hat{I}_{i\theta}$ consists of two regions; each visible bar has the same input strength. (B) Model output for (A), showing non-uniform output strengths (temporal averages of $g_x(x_{i\theta})$) for the edges. The input and output strengths are proportional to the bar widths. Because of the noise in the system, the saliencies of the bars in the same column are not exactly the same, this is also the case in other figures. (C) Output strengths (saliencies) averaged within each column versus lateral locations of the columns in (B), with the bar lengths proportional to the corresponding averaged output strengths. (D) The thresholded output from (B) for illustration, $thre = 0.5$. Boundary saliency measures $(r, z) = (3.7, 4.0)$.

Figure 4 shows examples using other orientations of the texture bars. The boundary strength decreases with decreasing orientation contrast at the region border. It is very weak when the orientation contrast is only 15° (figure 4(C))—here translation invariance in input is only weakly broken, making the boundary very difficult to detect pre-attentively. Note also that the most salient location in an image may not be exactly on the boundary (figure 4(C), see also figure 5(C)), this should lead to a bias in the estimation of the border location, and this can also be tested experimentally. This reinforces the point that outputs from pre-attentive segmentation need to be processed further by the visual system.

This model also copes well with textures defined by complex or stochastic patterns (figure 5). In figures 5(A–C) the neighbouring regions can be segmented even though they have the same bar primitives and densities. In particular, the two regions in figure 5(A) (or figure 5(C)) have exactly the same features, just like that in figure 1, and would be difficult to segment using traditional approaches. The model detects the true boundary in figure 5(D) even though there are orientation contrasts at many locations within each region. These examples work because the model is designed to detect where input homogeneity or translation invariance breaks down. In the example of figure 5(D), any particular vertical bar, within the right region far enough away from the border, has exactly the same contextual surround as any other vertical

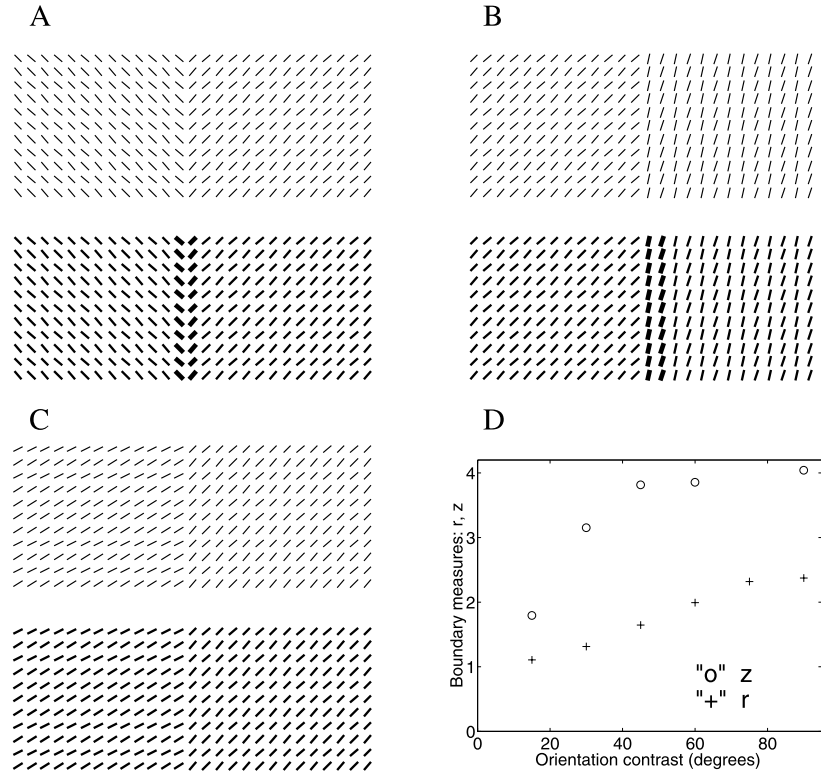


Figure 4. (A), (B), (C) Additional examples of model segmentation. Each is an input image as in figure 3(A) followed immediately below by the corresponding model outputs as in figure 3(B). In (A), (B), (C), respectively, the boundary measures are: $(r, z) = (1.4, 3.4)$, $(r, z) = (1.7, 3.7)$, $(r, z) = (1.03, 0.78)$. (D) The model segmentation performance, as measured by the boundary measure r, z (indicated by '+' and 'O', respectively), versus the orientation contrast at the texture border. Each data point is the average of all possible pairs of orientations of the two textures given an orientation contrast at the border. Again, each plotted region is only a small part of a larger extended image. The most salient column in (B) is, in fact, not exactly on the boundary, though the boundary column is only 6% less salient than its neighbour on the right, and $\sim 70\%$ more salient than areas away from the boundary. (C) contains two regions whose bar elements differ only slightly in orientation, the boundary bars are among the most salient ones, but only a very small fraction more salient than other bars (imperceptible in the line widths plotted in the output).

bar away from the border, i.e. they are all within the homogeneous or translation-invariant part of the region. Thus no one of such vertical bars will induce a higher response than any other, since they have the same direct input and the same contextual inputs. The same argument applies to the oblique bars or horizontal bars far away from the border in figure 5(D) as well as in figures 5(A–C). However, the bars at or near the border do not have the same contextual surround (i.e. contextual inputs) as those of the other bars, i.e. the homogeneity is truly broken, and thus they will induce a different response. By design, the border response will be higher. In other words, the model, with its translation-invariant horizontal connection pattern, only detects where input homogeneity breaks down, and the pattern complexity within a region does not matter as long as the region is homogeneous. The stochasticity in figure 5(E) implies a non-uniform response pattern even within each region. In that case, the border induces the

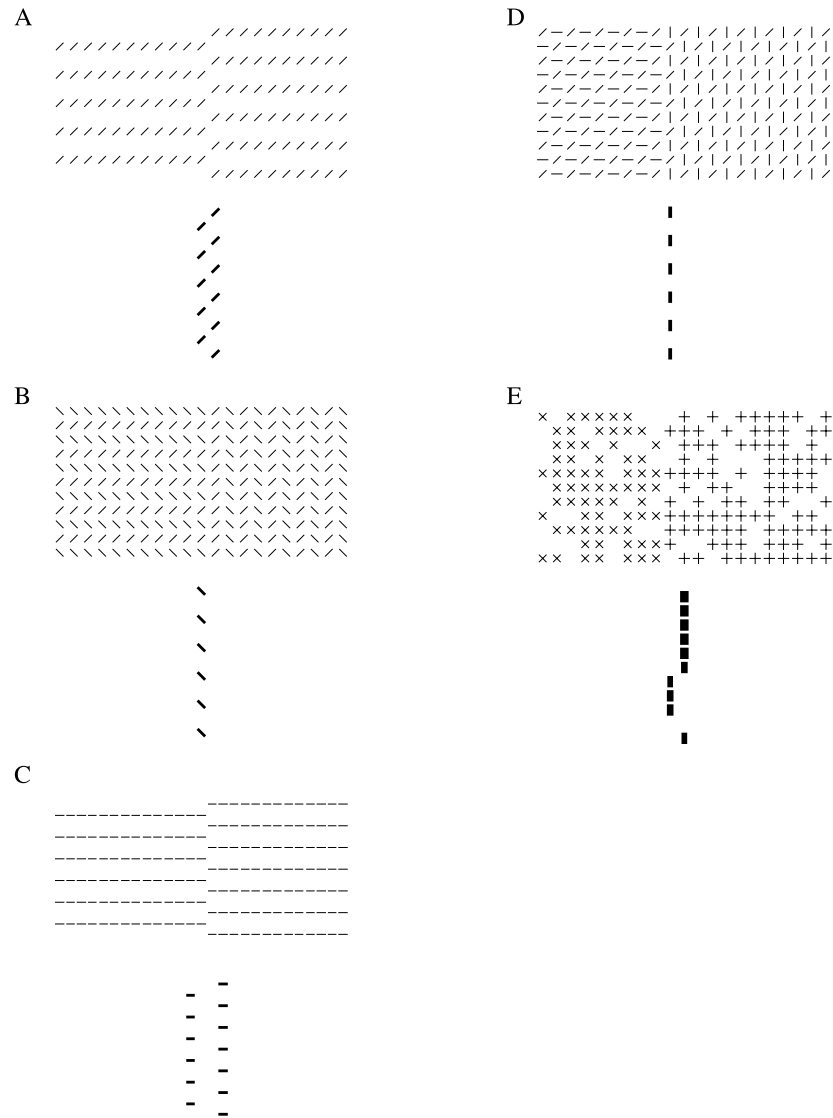
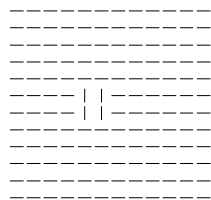


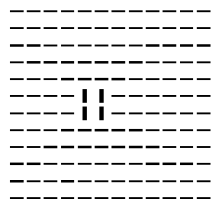
Figure 5. (A), (B), (C), (D) Model performance on regions with complex texture elements, and (E) regions with stochastic texture elements. Each plot is the model input ($\hat{I}_{i\theta}$) followed immediately below by the output ($g_x(x_{i\theta})$) highlights. For (A), (B), (C), (D), (E), respectively, the boundary measures are $(r, z) = (1.13, 3.5), (1.1, 1.5), (1.06, 2.6), (1.4, 2.9), (2.3, 3.3)$, the thresholds to generate the output highlights are $thre = 0.91, 0.9, 0.94, 0.85, 0.56$. In (C), even though the boundary saliency is only a fraction higher than others, this fraction is significant since it is $z = 2.6$ deviations away from the mean saliency.

highest response because it is where homogeneity breaks most strongly (see figure 9 for more examples of input randomness). The vertical array of highlights in figure 5(C) may correspond to the physiologically observed responses of V1 to illusory contours, i.e. the perceptual vertical contour without its corresponding vertical contour in the image (Grosf *et al* 1993). Note, however, that the most salient output in figure 5(C) is shifted a little away from the region

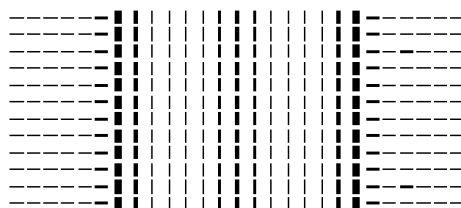
A



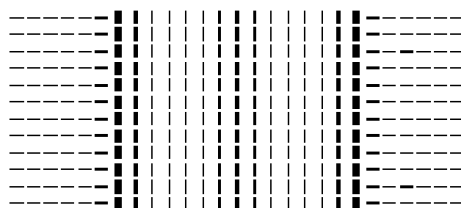
Output



B



Output



A : Cross among bars

B : Bar among crosses

Output

Output

The model replicates the results of physiological experiments on contextual influences from beyond the classical receptive field (Knierim and van Essen 1992, Kapadia *et al* 1995). In particular, figures 8(A–D) demonstrate that the response of a neuron to a bar of preferred orientation in its receptive field is suppressed by a textured surround, but enhanced by collinear contextual bars that form a line. As observed experimentally (Knierim and van Essen 1992), suppression in the model is strongest when the surround bars are of the same orientation as the centre bar, is weaker when the surround bars have random orientations and is weakest when the surround bars are oriented orthogonally to the centre bar. The relative degree of suppression is quantitatively comparable to that of the orientation contrast cells observed physiologically (Knierim and van Essen 1992). Similarly, figure 8(D) closely simulates the enhancement effect observed physiologically (Kapadia *et al* 1995) when bars in the surround are aligned with the central bar to form a line.

In realistic situations, there are many sources of input randomnesses or noise (other than neural noise), arising either from the image sampling stage, i.e. the transformation from the grey-scale image to the filtered and sampled inputs to the pyramidal cells, or randomness in the input scenes themselves. The overall performance of our pre-attentive visual system depends on both the image sampling stage and the intra-cortical interaction stage. Since our model in its current implementation has a much sparser sampling than that in human vision, its problem of sampling noise (e.g. aliasing) is much more serious. A better visual system, such as the human visual system, should have a many-fold over-complete and much denser sampling, i.e. the sizes or the tuning widths of the receptive fields in space, orientation and spatial frequency, etc are much larger than the distance (in space, orientation and spatial frequency, etc) between two nearby sampling nodes. With such dense sampling, there will be little aliasing (in space, orientation, scale) and thus the sampling noise can be negligible compared to the noise in the visual scene itself. So far we have omitted the image sampling stage in the applications of our model by directly applying the accurate inputs $I_{i\theta}$ to the pyramidal cells. In this way, we can demonstrate the power of the intra-cortical interaction by isolating its effects, without having to build an almost perfect and many-fold over-complete sampling stage and thus many more pyramidal cells in the model, whose computer simulation would overwhelm my currently available computing power. By introducing noise and variations in input $I_{i\theta}$ to the pyramidal cells, figure 9 shows that the texture boundary or the pop-out strength decreases if the orientations and/or the input strengths of the texture elements are somewhat random or the spacing between the elements increases. Boundary detection or figure pop-out in the model is difficult when orientation noise $>30^\circ$ or when the spacing between bar elements is more than four or five grid points (or texture element sizes). The qualitative and quantitative performances of the model on the cut-off orientation contrast, orientation noise and bar spacings compare reasonably well with human performance on segmentation related tasks (Nothdurft 1985, 1991, Li 1999b). This means that, if the input randomness is caused by the unsatisfactory sampling and filtering stage (the transform from grey-scale images to $I_{i\theta}$) in the model, then the degradation in the model performance is comparable with that of the human performance with equivalently degraded input scenes. The graceful degradation of the model's segmentation performance with the noise in input strengths, orientations and positions of the image elements (figure 5(E)) generally applies to all kinds of input patterns, including the ones in this paper. In fact, the temporal behaviour of the model, e.g. the neural response synchrony between elements of the same texture patch in figure 9 (although this is not used for segmentation purposes in this paper), changes only very mildly or negligibly when the added randomness is not enough to destroy the segmentation performance. Figure 10 demonstrates the current model performance on a photograph. The effects of single-scale sampling and the noise arising from the sparse sampling (aliasing) are apparent in the model input image,

A: Iso-orientation

C: Random background

Output

Output

B: Cross orientation

D: Line and noise

Input ($\hat{I}_{i\theta}$)

Output

Out

A: two texture region input
with orientation jitter 15°

Model output

Model output

Model output

Model ou

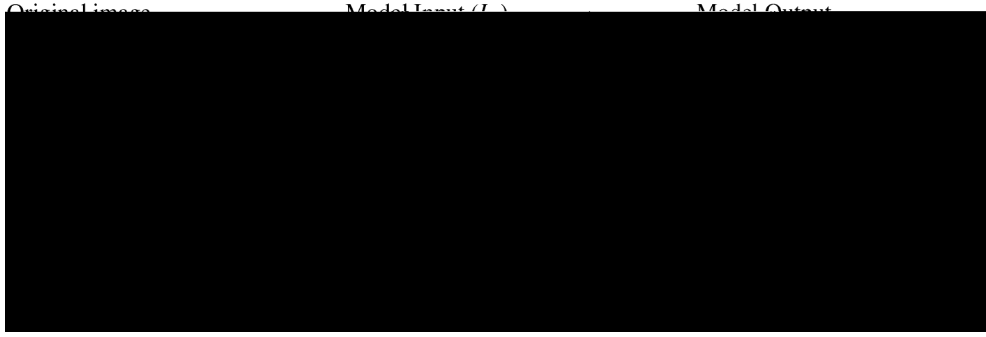


Figure 10. Model behaviour on a photographic image composed of 126×129 pixels. The input to the model is modelled as $I_{i\theta} = (e^2 + o^2)^{1/4}$, where e and o are the outputs from the even and odd Gabor-like filters at grid sampling points i with preferred orientation θ , the power $\frac{1}{4}$ coarsely models some degree of contrast gain control. The sampling points i are spaced three pixels apart from the neighbours vertically or horizontally, the Gabor filters are of the form $\exp(-(4y^2 + x^2)/26) \cos(1.4y)$ and $\exp(-(4y^2 + x^2)/26) \sin(1.4y)$, where x and y are measured in pixels. At each grid point, bars of almost all $K = 12$ orientations have non-zero input values $I_{i\theta}$. For display clarity, no more than two strongest input or output orientations are plotted at each grid point in model input and output above. The second orientation bar is plotted only if input or output values at the grid point are not uni-modal, and the second strongest modal is at least 30% in strength of the strongest one. The strongest $I_{i\theta} = 3.0$ in the whole input. The more salient locations in the model output include some vertical borders of the columns in the input texture, as well as horizontal streaks, which are often also conspicuous in the original image. Note that this photograph is sampled against a blank background on the left and right, hence the left and right sides of the photograph area are also highlighted.

5. Summary and discussions

5.1. Summary of the results

In this paper, we first proposed that contextual influences in V1 serve pre-attentive segmentation by highlighting the important image locations. Secondly, we validated this by presenting a biologically based model, which implements segmentation. The model can easily handle some segmentation examples such as those in figure 5(A) (in which the two regions have the same texture features and the region border does not have a definite edge signal) that pose problems for traditional approaches, but are easily segmentable by human pre-attentive vision.

This is the first model of V1 that captures the effect that neural activities are higher near region boundaries, as well as the natural consequence of this on pop-out of small figures against backgrounds and asymmetries in pop-out strengths between alternative choices of figure and ground. Underlying the model are the *local* intra-cortical interactions that modify individual neural activities depending on the contextual visual stimuli, thus detecting the region boundaries by detecting the breakdown of translation invariance in inputs. Furthermore, the model uses the same neural circuit for both the region boundary effect and contour enhancement—individual contours in a noisy or non-noisy background can also be seen as examples of the breakdown of translation invariance in inputs. Putting these effects together, V1 is modelled as a saliency network that highlights the conspicuous image areas in inputs. These conspicuous areas include region boundaries, and smooth contours or small figures against backgrounds, thus serving the purpose of pre-attentive segmentation. This V1 model, with its intra-cortical interactions designed for pre-attentive segmentation, successfully explains the contextual influences beyond the classical receptive fields observed in physiological

experiments (Knierim and van Essen 1992, Kapadia *et al* 1995). Hence, we suggest that one of the main roles for contextual influences is pre-attentive segmentation.

5.2. Relation to other studies

It has recently been argued that texture analysis is performed at low levels of visual processing (Bergen 1991)—indeed, filter-based models (Bergen and Adelson 1988) and their nonlinear extensions (e.g. Malik and Perona 1990) capture well much of the phenomenology of psycho-physical performance. However, these previous segmentation models use a region-based approach, i.e. locating the border by classifying the region textures first, and thus differ from our model in principle. For example, the texture segmentation model of Malik and Perona (1990) also employs neural-like interactions in a parallel network. However, their interactions are designed to *classify* or extract region features. Consequently, the model requires a subsequent feature comparison operation (by spatial differentiation) in order to segment. It would thus have difficulties in cases like figure 1, and would not naturally capture figure pop-out, asymmetries between the figure and ground, or contour enhancement.

The task of locating conspicuous image locations without specific tuning to (or classification of) any region features is significantly more sophisticated computationally than standard early visual processing using centre-surround filters (which would not be able to detect boundaries between two different texture regions with the same mean luminance) or the like (Marr 1982). While the early stage filters code image primitives (Marr 1982), our mechanism should help in object surface representation. Since they collect contextual influences over a whole neighbourhood, the neurons naturally account for the statistical nature of the local image characteristics that define regions. This agrees with Julesz's conjecture of segmentation by image statistics (Julesz 1962) without any restriction to being sensitive only to the first- and second-order image statistics. Julesz's concept of textons (Julesz 1981) could be viewed within this framework as any feature to which the particular intra-cortical interactions are sensitive and discriminatory. Using orientation-dependent interactions between neurons, the model agrees with previous ideas (Northdurft 1994) that (texture) segmentation is primarily driven by orientation contrast. However, the emergent network behaviour is collective and accommodates characteristics of general regions beyond elementary orientations, as in figure 5. Furthermore, the psycho-physical phenomena of filling-in (when one fails to notice a small blank region within a textured region) could be viewed as the instances when the network fails to sufficiently highlight the non-homogeneity in inputs near the filled-in area.

Our basic framework is quite primitive. It merely segments surface regions from each other, whether or not these regions belong to different visual objects. Furthermore, by segmenting under a boundary/border-based approach without classifying region features, it does not characterize the region properties (such as by the $(2 + 1)$ /two-dimensional surface representations (Marr 1982)) more than what is already implicitly present in the raw image pixels or the cell responses in V1. Hence, for example, the model output does not indicate whether a region is made of a transparent surface on top of another surface.

Key support for the model comes from experimental evidence that pre-attentive segmentation precedes and is dissociated from visual classification/discrimination of surfaces and regions. Recent experimental evidence from V1 (Lamme *et al* 1997, Zipser 1998) shows that the modulation of neural activities starts at texture boundaries and only later includes figure surfaces, where the neural modulations take about 50 ms to develop after the initial cell responses (Zipser *et al* 1996, Zipser 1998). Some psycho-physical evidence (Scialfa and Joffe 1995) suggests that information regarding (figure) target presence is available before information regarding feature values of the targets. Also consistent with the model is that V2

lesions in monkeys are shown to disrupt region content discrimination but not region border detection (Merigan *et al* 1993). Furthermore, neural modulation in V1, especially at figure surfaces (Zipser 1998), is strongly reduced or abolished by anaesthesia or lesions in higher visual areas (Lamme *et al* 1997), while experiments by Gallant *et al* (1995) show that activity

target bar. The perceived orientation of the target bar could shift away or towards the orientation of the contextual bars, depending on the spatial arrangement (and the orientations) of the contextual bars. This is in contrast to the usual notion that the orientation of the target bar tends to shift away from those of the contextual bars. Both our model and a recent psycho-physical study (Kapadia 1998) confirm such context-dependent distortion in perceived orientation. V1 cells do display changes in orientation tuning under contextual influences (Gilbert and Wiesel 1990), although the magnitude and direction of the changes vary from cell to cell.

5.3. Comparison with other models

There are many other related models. Many cortical models are mainly concerned with contour linking, and Li (1998b) has a detailed citation of these models and comparisons with our model. For instance, Grossberg and his colleagues have developed models of visual cortex over many years (Grossberg and Mingolla 1985, Grossberg *et al* 1997). They proposed a ‘boundary contour system’ as a model of intra-cortical and inter-areal neural interactions in V1 and V2 and feedback from V2 to V1. The model aims to capture illusory contours, which link line segments and line endings, and the authors claim that such linking affects segmentation. Other models are more concerned with regions, namely, to classify region features and then to segment regions by comparing the classifications. To obtain texture region features, Malik and Perona (1990) use local intra-cortical inhibition. Geman and Geman built a model based on Markov random fields to restore images, in which neighbouring image features influence each other statistically (Geman and Geman 1984). Such local interactions improve the outcomes from the prior and preliminary feature classifications to drive segmentation.

Our model contrasts with previous models by modelling the effect of region boundary highlights in V1, and by using the same neural circuit as used for contour enhancement. Equally, its instantiation in V1 means that our model does not perform operations such as the classification and smoothing of region features and the sharpening of boundaries as carried out in some other models (e.g. Lee 1995, Malik and Perona 1990). There are many other models of visual processing (e.g. Grossberg and Mingolla 1985, Zucker *et al* 1989, Yen and Finkel 1997) that use a bow-tie-shaped interaction pattern that is qualitatively similar to ours (figure 2(B)). This, however, does not mean that those models would necessarily perform the same computations as our model. Using dynamic systems theory, a recent work (Li and Dayan 1999) has shown that if the units in the network interact with each other directly and reciprocally (or symmetrically in the terminology of recurrent neural networks), as in the models of Grossberg, Zucker and co-workers, the network cannot produce the desired contour enhancement and (texture) boundary highlighting even with the same qualitative pattern of interactions. In particular, the three design conditions (in section 3 or the appendix) for the synaptic weights are not likely to be satisfied simultaneously in those networks without significantly compromising the selective enhancement of the contours and texture borders. In other words, if those networks enhance the contours or texture boundaries sufficiently, then they are likely also to hallucinate illusory boundary or contour highlights even when there is none in input. Apparently, the biological fact that the principal (pyramidal) cells inhibit each other indirectly via inhibitory interneurons offers significant dynamic advantages over the seemingly simpler but less plausible networks with direct and reciprocal inhibition.

5.4. Limitations and extensions of the model

The model is still very primitive compared to the true complexity of V1. We have yet to include multiscale sampling or the over-complete input sampling strategy adopted by V1, or to

include colour, time or stereo input dimensions. Also, the receptive field features used for the bar/edges should be determined more precisely. The details of the intra-cortical circuits within and between hypercolumns should also be better determined to match biological vision.

Multiscale sampling is needed not only because images contain multiscale features, but also to model V1 responses to images from flat surfaces slanted in depth—such a region should also be seen as ‘homogeneous’ or ‘translation invariant’ by V1, such that it has uniform saliency. Merely replicating and scaling the current model to multiple scales is not sufficient for this purpose. The computation requires interactions between different scales. We also have yet to find a better sampling distribution even within a single scale. Currently, the model neurons within the same hypercolumn have exactly the same RF centres and the RFs from different hypercolumns do not overlap. This sampling arrangement is much sparser than the V1 sampling.

In addition to orientation and spatial location, neurons in V1 are tuned for motion direction/speed, disparity, ocularity, scale and colour (Hubel and Wiesel 1962, Livingstone and Hubel 1984). Our model should be extended to these dimensions. The horizontal connections in the extended model will link edge segments with compatible selectivities to all of these facets as well as orientation, as suggested by experimental data (e.g. Li and Li 1994, Gilbert 1992, Ts'o and Gilbert 1988). The model should also be expanded to include details such as on and off cells, cells of different RF phases, non-orientation selective cells, end stopped cells and more cell layers. These details should lead to better quantitative match between the model and human vision.

Any given neural interaction will be more sensitive to some region differences than others. Therefore, the model sometimes finds it easier or more difficult to segment some regions than natural vision. Physiological and psycho-physical measurements of the boundary effect for different types of textures can help to constrain the connection patterns in an improved model. Experiments also suggest that the connections may be learnable or plastic (Karni and Sagi 1991, Sireteanu and Rieth 1992, Polat and Sagi 1994). It is also desirable to study the learning algorithms to develop the connections.

We currently model saliency at each location quite coarsely by the activity of the most salient bar. It is mainly an experimental question as to how to best determine the saliency, and the model should be modified accordingly. This is particularly the case once the model includes multiple scales, non-orientation selective cells and other visual input dimensions. The activities from different channels should somehow be combined to determine the saliency at each location of the visual field.

In summary, this paper proposes a computational framework for pre-attentive segmentation in the primary visual cortex. It introduces a simple and biologically plausible model of V1 to implement the framework using mechanisms of contextual influences via intra-cortical interactions. Although the model is as yet very primitive compared to the real cortex, our results show the feasibility of the underlying ideas, that breakdown of input translation invariance can be used to segment regions, that region segmentation and contour detection can be addressed by the same mechanism, and that low-level processing in V1 together with *local* contextual interactions can contribute significantly to visual computations at *global* scales.

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Appendix

A.1. Design analysis for horizontal connections

Connections J and W are designed to satisfy the three conditions listed in section 3. To illustrate the design for conditions (1) and (2), consider the example of a homogeneous input

$$I_{i\theta} = \begin{cases} I_o > 0 & \text{when } \theta = \theta_o \\ 0 & \text{otherwise} \end{cases} \quad (\text{A1})$$

of a bar oriented θ_o at every sampling point. By symmetry, a mean field solution $(\bar{x}_{i\theta}, \bar{y}_{i\theta})$ is also independent of spatial location i . For simplicity assume $\bar{x}_{i\theta} = 0$ for $\theta \neq \theta_o$, and ignore all $(x_{i\theta}, y_{i\theta})$ with $\theta \neq \theta_o$. To study whether this mean field solution $(\bar{x}_{i\theta_o}, \bar{y}_{i\theta_o})$ is stable, look at the perturbations $(x'_i \equiv x_{i\theta_o} - \bar{x}_{i\theta_o}, y'_i \equiv y_{i\theta_o} - \bar{y}_{i\theta_o})$ around it. It follows that

$$\dot{Z} = AZ \quad (\text{A2})$$

where $Z = (x'^T, y'^T)^T$. Matrix A results from expanding equations (1) and (2) around the mean field solution, it contains the horizontal connections $J_{i\theta_o, j\theta_o}$ and $W_{i\theta_o, j\theta_o}$ linking bar segments oriented all at θ_o . Translation invariance in J and W implies that every eigenvector of A is a cosine wave in space for both x' and y' . To ensure condition (1), either every eigenvalue of A should be negative so that the mean field solution is stable and no perturbation from the homogeneous mean field solution is self-sustaining, or the eigenvalue with largest positive real part should correspond to the zero-frequency cosine wave in space. In the latter case, the deviation or perturbation from the mean field solution tends to be homogeneous, and thus does not spontaneously form non-homogeneous spatial patterns, although it will oscillate over time (Li 1998b). Iso-orientation suppression under supra-threshold input I_o is used to satisfy condition (2). This requires that every pyramidal cell $x_{i\theta_o}$ in an iso-orientation surround should receive stronger overall disynaptic inhibition than monosynaptic excitation:

$$\sigma \sum_j W_{i\theta_o, j\theta_o} > \sum_j J_{i\theta_o, j\theta_o} \quad (\text{A3})$$

where $\sigma \equiv \psi(0)g'_y(\bar{y}_{i\theta_o})$ comes from the inhibitory interneurons. The excitatory cells near a region boundary lack a complete iso-orientation surround, they are less suppressed and so exhibit stronger responses, meeting condition (2). We tested conditions (1) and (2) in simulations using these simple and other general input configurations including the cases when input within a region is of the form $I_{i\theta} \equiv \tilde{I}_\theta$, where $\tilde{I}_\theta$ is non-zero for two orientation indices θ . The design to ensure condition (3) that the system should properly enhance isolated smooth contours has been shown in Li (1998b) which, to avoid an over-long manuscript, did not discuss conditions (1) and (2). Briefly, condition (3) is ensured by strong enough but limited strength monosynaptic excitation $\sum_{j\theta' \in \text{contour}} J_{i\theta, j\theta'}$ along any smooth contour extending from $i\theta$ —to give enough enhancement without exciting any bar/edge elements beyond the end of non-closed contours—and enough disynaptic inhibition between local, similarly oriented and non-aligned bars—to avoid enhancement of the noisy background.

A.2. A complete list of model parameters

One can use the following parameters to reproduce all results in the paper, using equations (1) and (2):

$$\alpha_x = \alpha_y = 1 \quad K = 12$$

$$g_x(x) = \begin{cases} 0 & \text{if } x < T_x \\ (x - T_x) & \text{if } T_x \leq x \leq T_x + 1 \\ 1 & \text{if } x > T_x + 1 \end{cases}$$

$$g_y(y) = \begin{cases} 0 & \text{if } y < 0 \\ g_1 y & \text{if } 0 \leq y \leq L_y \\ g_1 L_y + g_2(y - L_y) & \text{if } 0 < L_y \leq y \end{cases}$$

$$T_x = 1 \quad L_y = 1.2 \quad g_1 = 0.21 \quad g_2 = 2.5$$

$$\psi(\theta) = \begin{cases} 1 & \text{when } \theta = 0 \\ 0.8 & \text{when } |\theta| = \pi/K = 15^\circ \\ 0.7 & \text{when } |\theta| = 2\pi/K = 30^\circ \\ 0 & \text{otherwise} \end{cases}$$

$$I_c = 1.0 + I_{\text{noise}}$$

$$I_o = 0.85 + I_{\text{normalization}} + I_{\text{noise}}$$

$$I_{\text{normalization}}(i\theta) = -2.0 \left[\frac{\sum_{j \in S_i} \sum_{\theta'} g_x(x_{j\theta'})}{\sum_{j \in S_i} 1} \right]^2$$

S_i = all j such that $|i - j| \leq 2$ grid distances

I_{noise} = zero mean, random, mean temporal width 0.1, mean amplitude 0.1

$$J_o = 0.8$$

$$J_{i\theta, j\theta'} = \begin{cases} 0.126e^{-(\beta/d)^2 - 2(\beta/d)^7 - d^2/90} & \text{if } 0 < d \leq 10.0 \text{ and } \beta < \pi/2.69 \\ & \text{or } 0 < d \leq 10.0 \text{ and } \beta < \pi/1.1 \\ & \text{and } |\theta_1| < \pi/5.9 \text{ and } |\theta_2| < \pi/5.9 \\ 0 & \text{otherwise} \end{cases}$$

$$W_{i\theta, j\theta'} = \begin{cases} 0 & \text{if } d = 0 \text{ or } d \geq 10 \text{ or } \beta < \pi/1.1 \\ & \text{or } |\Delta\theta| \geq \pi/3 \text{ or } |\theta_1| < \pi/11.999 \\ 0.14(1 - e^{-0.4(\beta/d)^{1.5}})e^{-(\Delta\theta/(\pi/4))^{1.5}} & \text{otherwise.} \end{cases}$$

The parameters d , β and $\Delta\theta$ in the expressions for $J_{i\theta, j\theta'}$ and $W_{i\theta, j\theta'}$ are determined as follows. Let $|i - j| = d$, and denote the angles between the edge elements and the line $i - j$ by θ_1 and θ_2 , where $|\theta_1| \leq |\theta_2| \leq \pi/2$ and $\theta_{1,2}$ are positive or negative depending on whether the edges rotate clockwise or counter-clockwise towards the connecting line $i - j$ in no more than a $\pi/2$ angle. Denote $\beta = 2|\theta_1| + 2\sin(|\theta_1 + \theta_2|)$, $\Delta\theta = \theta - \theta'$ with $|\theta - \theta'| \leq \pi/2$. These same parameters were listed in Li (1998b).

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