

## (Abstract) neural representations of spaces and concepts

Neil Burgess  
Institute of Cognitive Neuroscience  
University College London



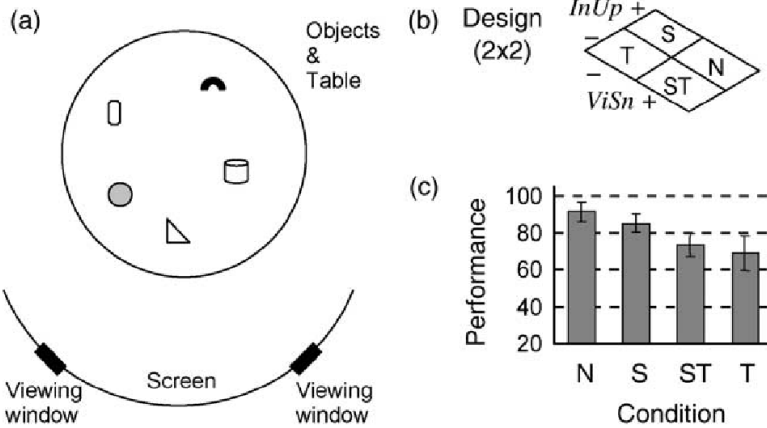
### *Abstract neural representations*

- 1) *Frames of reference for spatial representation*
- 2) *Place cells & boundary vector cells*
- 3) *Neural level model of Spatial Memory and Imagery*
- 4) *Place and grid cells, environmental and self-motion inputs?*
- 5) *Grid cells as dynamic imagery?*
- 6) *Place and grid cells, representing states and transitions for planning?*

### Multiple parallel representations in spatial memory.

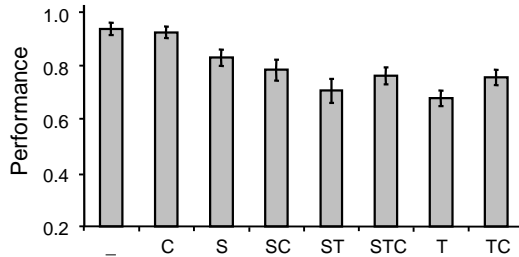
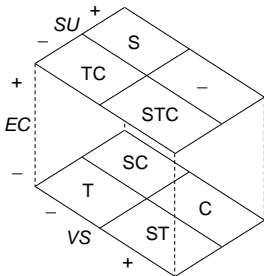
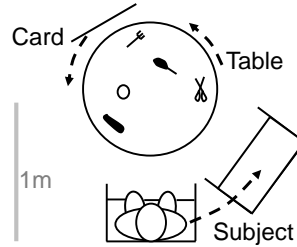
Effects of consistency with 'Visual Snapshots' & Internal 'Spatial Updating'

Wang & Simons 1999



### Multiple parallel representations in spatial memory.

Visual Snapshots (*egocentric*),  
Spatial Updating (*egocentric*) and  
External Cues (*allocentric*).



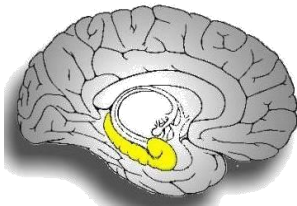
Burgess, Spiers, Paleologou, 2004

Consistency	InUp:	ViSn:	ExCu:
-	+	+	+
C	+	+	-
S	+	-	+
SC	+	-	-
ST	-	+	-
STC	-	+	+
T	-	-	-
TC	-	-	+

## Abstract neural representations

- 1) *Frames of reference for spatial representation*
- 2) **Place cells & boundary vector cells**
- 3) *Neural level model of Spatial Memory and Imagery*
- 4) *Place and grid cells, environmental and self-motion inputs?*
- 5) *Grid cells as dynamic imagery?*
- 6) *Place and grid cells, representing states and transitions for planning?*

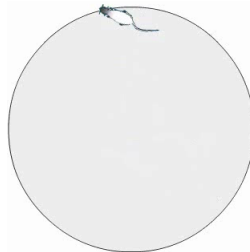
The hippocampus supports memory (e.g. HM), but how does it work?



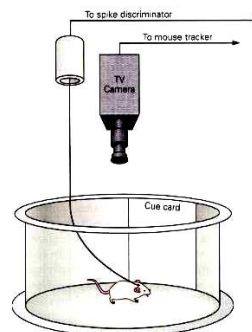
Spatial studies in rodents => likely neural representations.



Place cells- 'allocentric' location



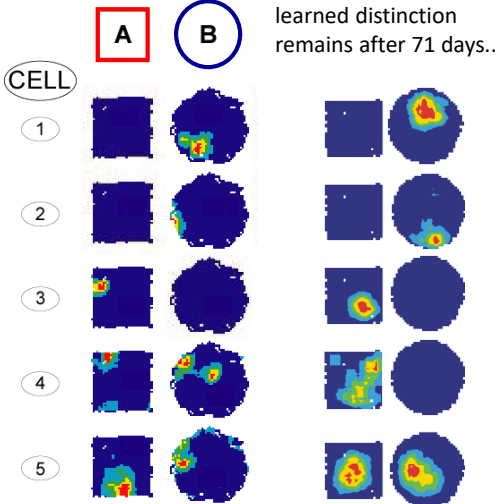
O'Keefe & Dostrovsky, 1971



Video by Julija Krupic

### Place cells show long term memory and pattern completion

Place cell "remapping:" long-term memory for highly distinct environments.



Place cell representation shows attractor dynamics

*Wills, Lever, Cacucci, Burgess, O'Keefe, 2005*

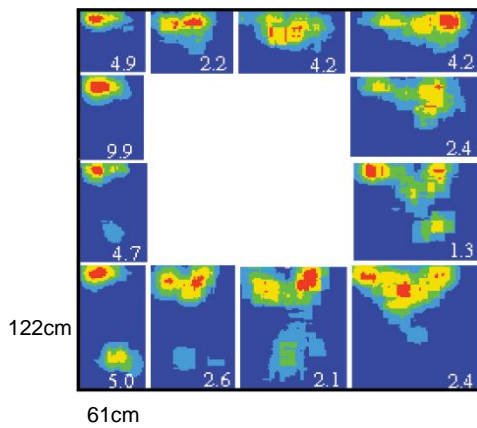
and 'pattern completion' depending on CA3 NMDA receptors

*Nakazawa et al., 2002*

*Lever, Wills, Cacucci, Burgess, O'Keefe, 2002*



### Environmental boundaries particularly influence place cell firing



*O'Keefe & Burgess (1996)*

### Place Cell firing as a thresholded sum of "Boundary Vector Cell" inputs

Boundary Vector Cells (BVCs)  
signal distance to boundary along an *allocentric* direction

Firing rate      Receptive field

environmental boundary

O'Keefe & Burgess, 1996; Hartley et al 2000

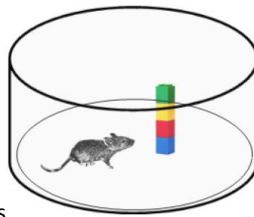
### BVCs found in subiculum & entorhinal cortex

Including those firing at a distance

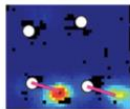
Steve Poulter & Colin Lever

Lever, Burton, Jeewajee, O'Keefe, Burgess, 2009  
See also Barry et al, 2006; Solstad et al, 2008

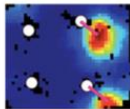
## Object Vector Cells



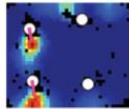
Recently found, in hippocampus



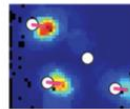
Unit 1



Unit 2



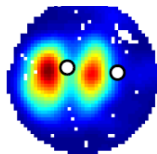
Unit 3



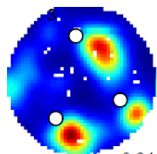
Unit 4

Desmukh & Knierim, 2013

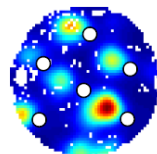
and medial entorhinal cortex



10.6 Hz



9.6 Hz



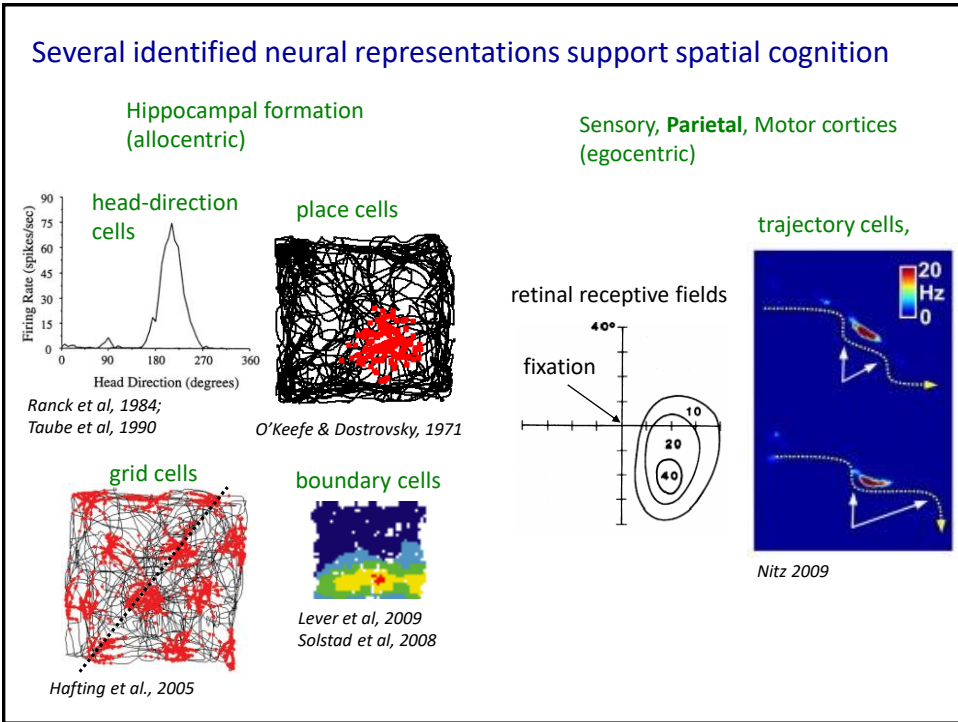
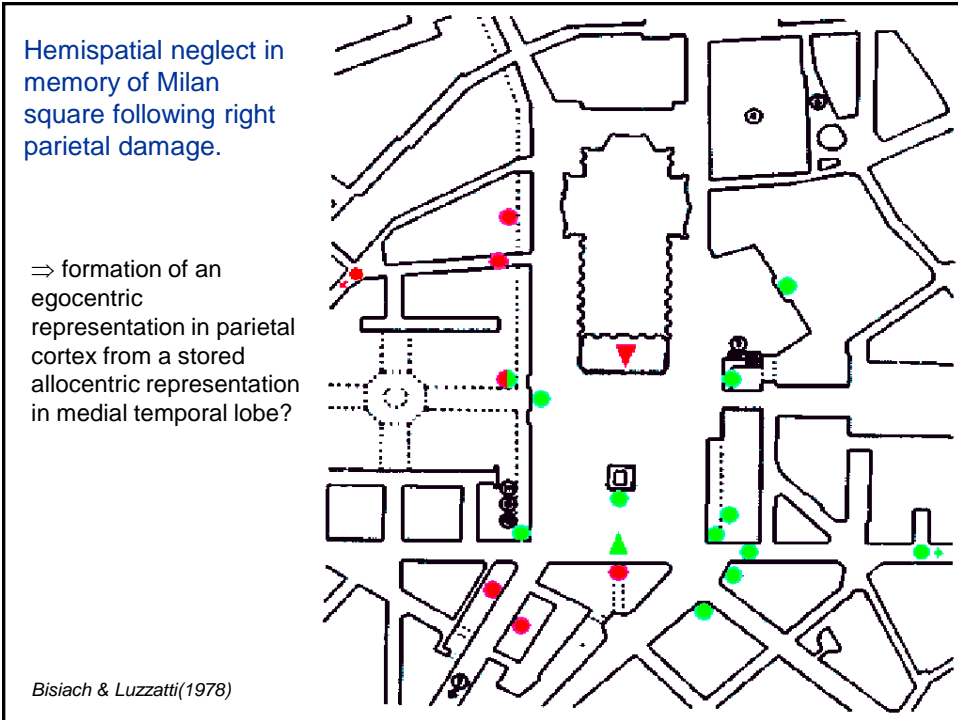
18.3 Hz

Hoydal..Moser 2019

Reviewed in Bicanski &  
Burgess, 2020

## *Abstract neural representations*

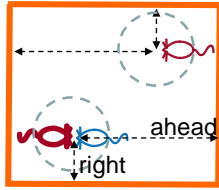
- 1) *Frames of reference for spatial representation*
- 2) *Place cells & boundary vector cells*
- 3) ***Neural level model of Spatial Memory and Imagery***
- 4) *Place and grid cells, environmental and self-motion inputs?*
- 5) *Grid cells as dynamic imagery?*
- 6) *Place and grid cells, representing states and transitions for planning?*



## Frames of reference for neural coding

*'egocentric'*

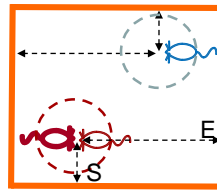
Body-centred location of objects



Perception  
Action/Imagery

*'allocentric'*

World-centred location of agent

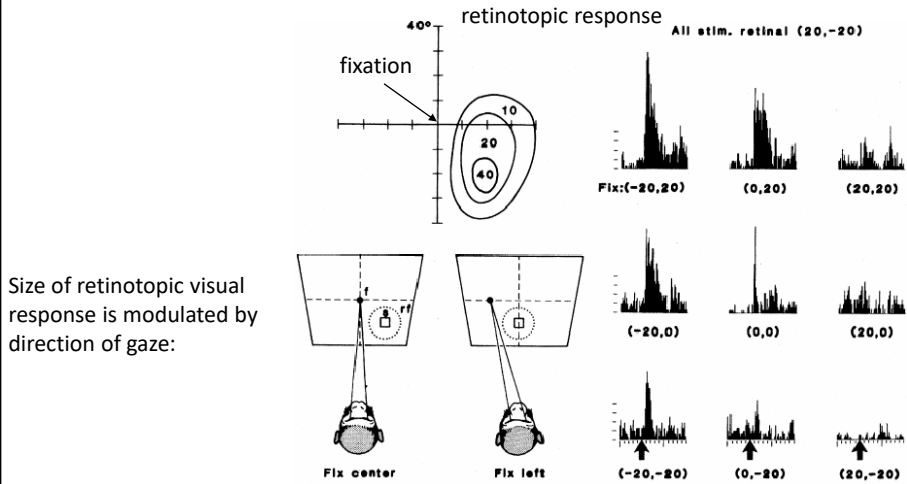


Place cells  
Head-direction cells

Burgess et al 2001

## 'Gain field' responses in posterior parietal cortex

i.e. conjunctive responses to (retinotopic) visual input  $\times$  gaze direction



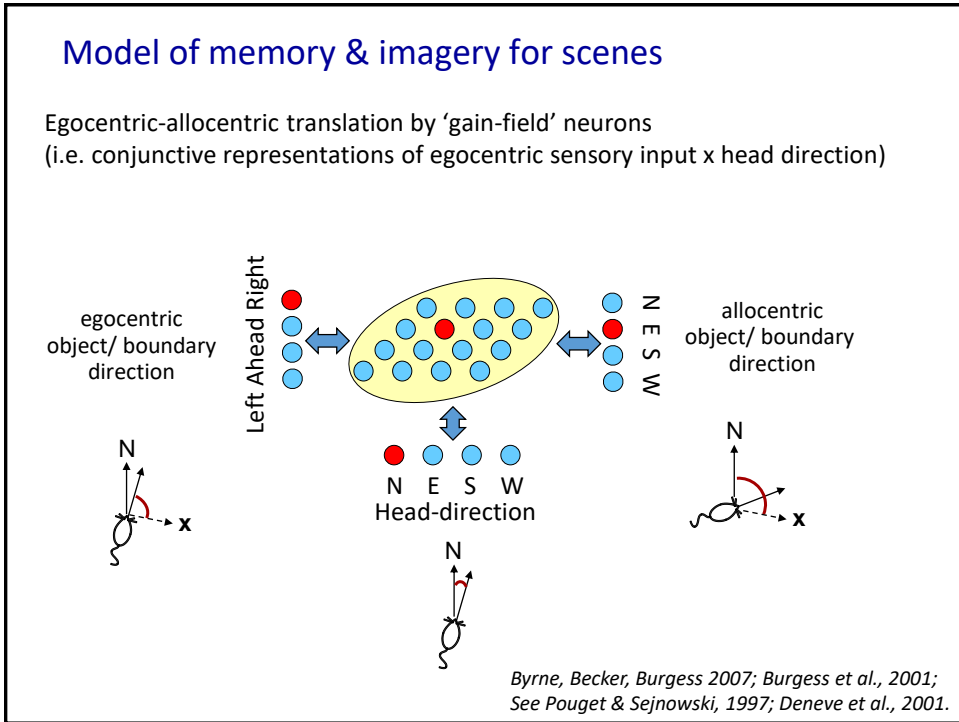
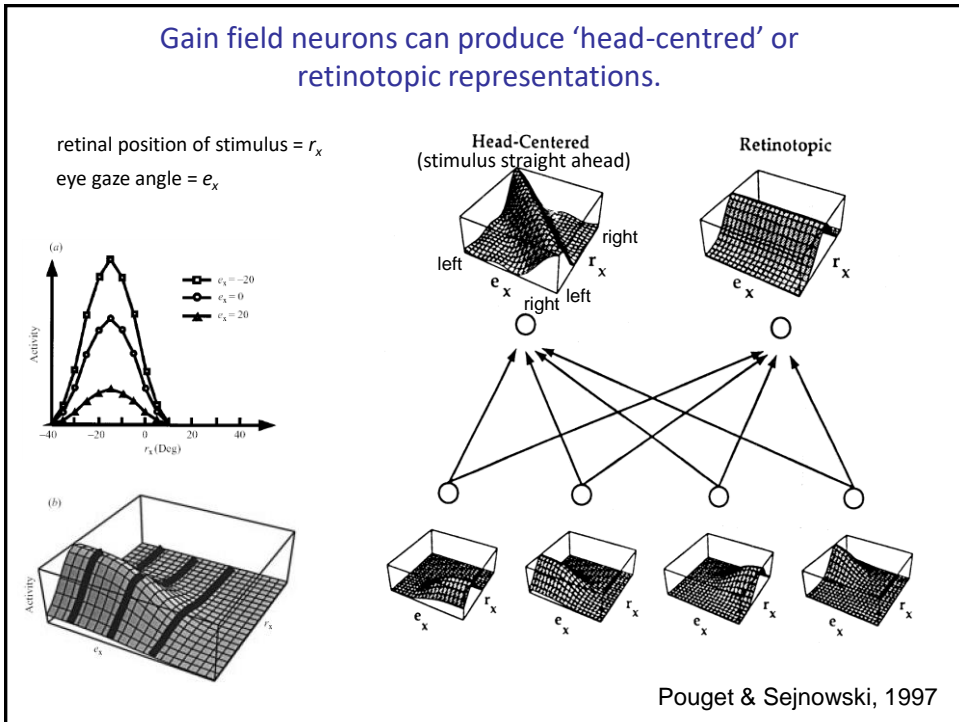
Size of retinotopic visual response is modulated by direction of gaze:

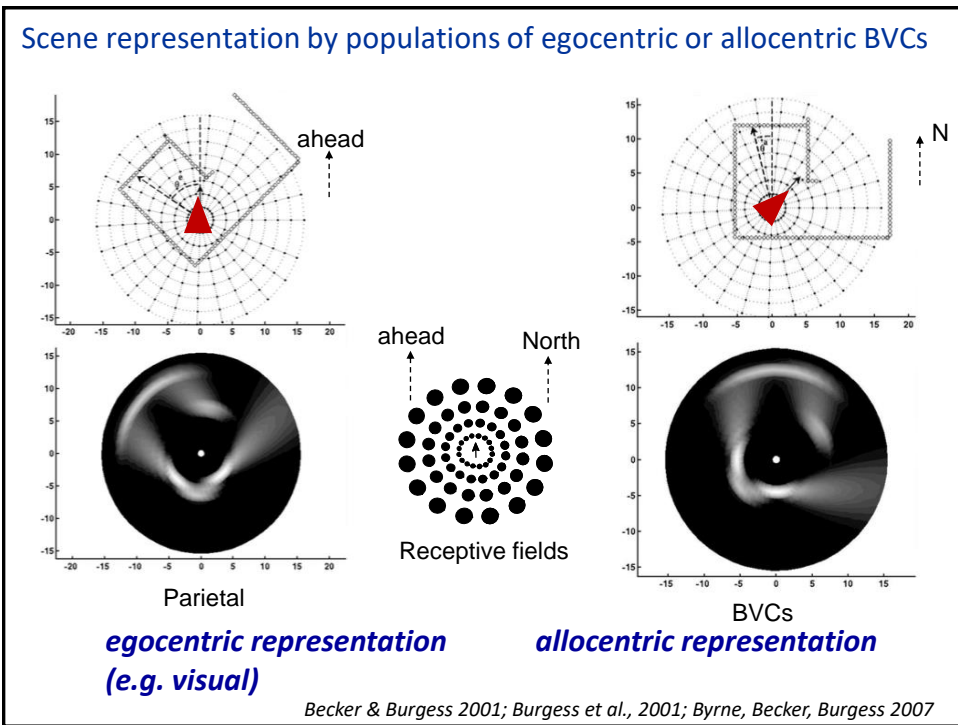
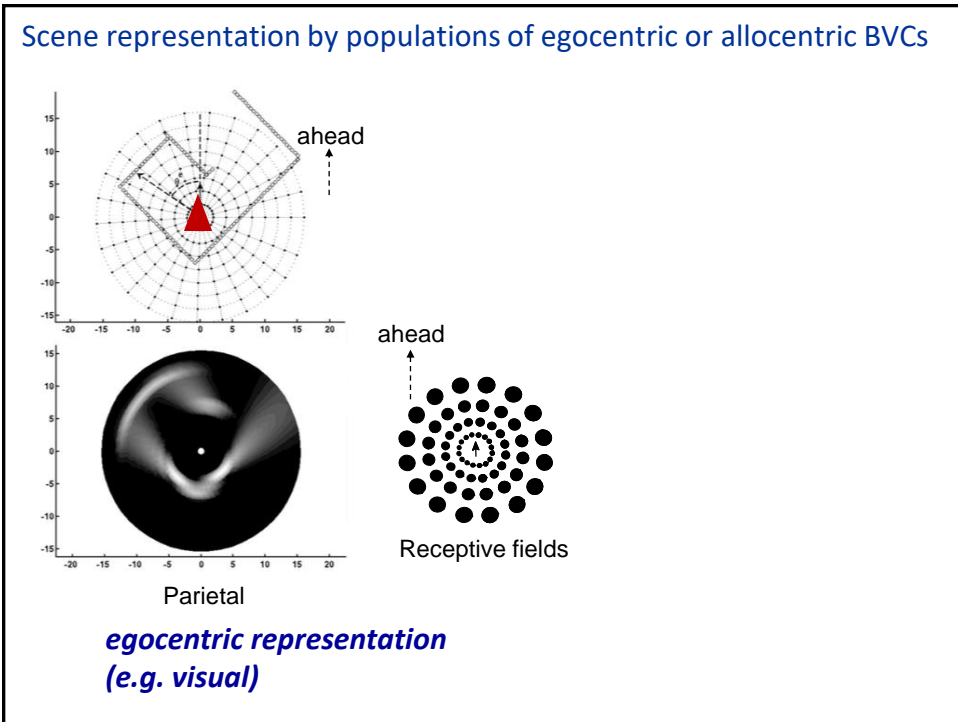
Andersen et al 1985

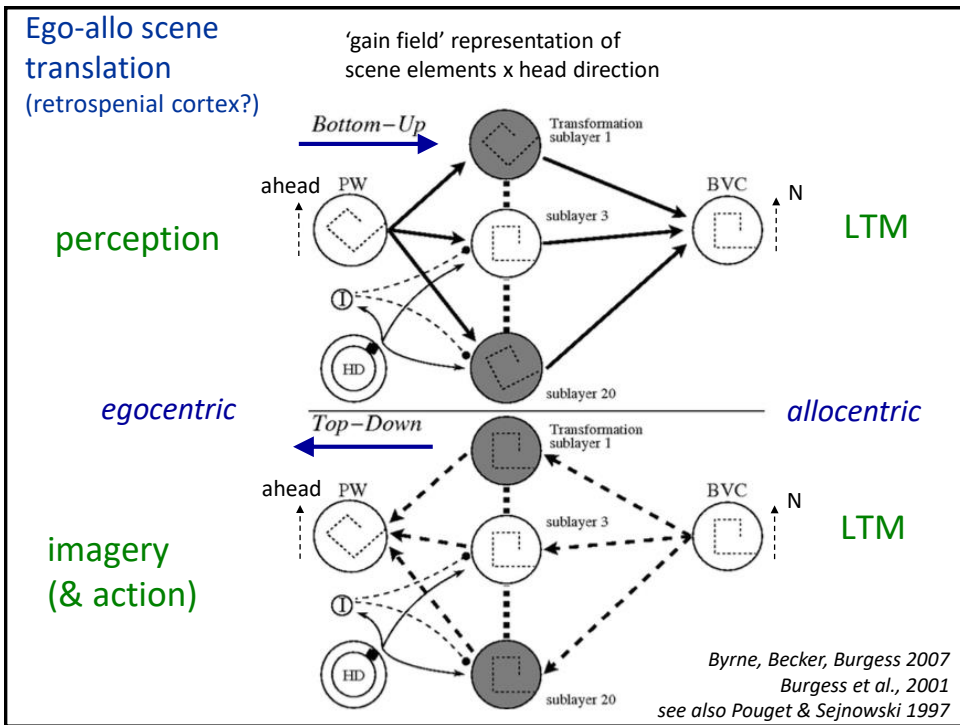
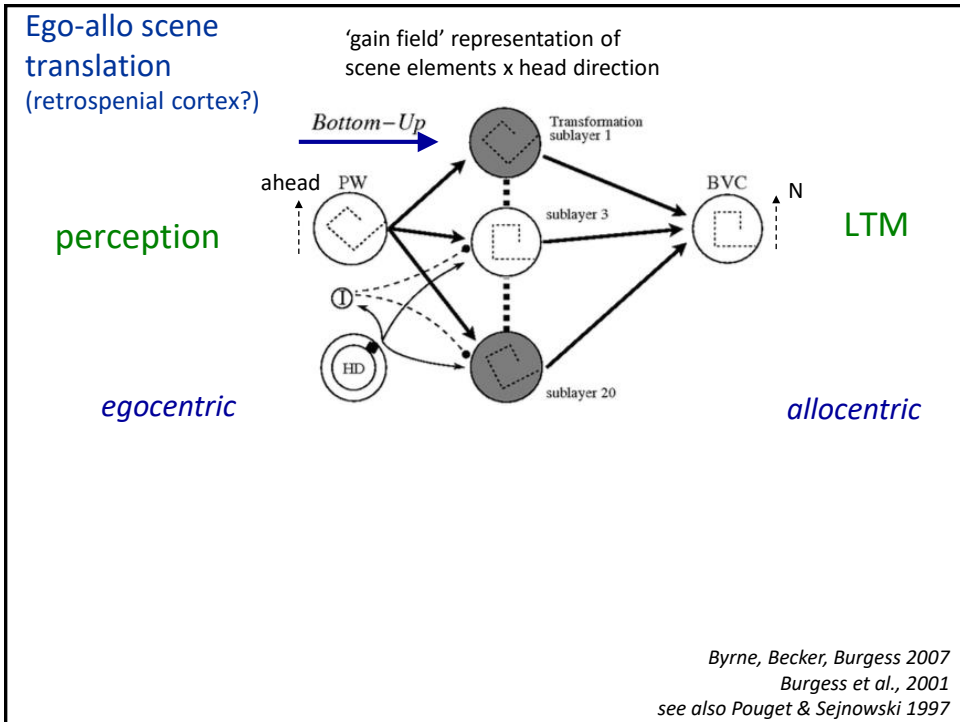
or by direction of the head (Snyder et al 1998).

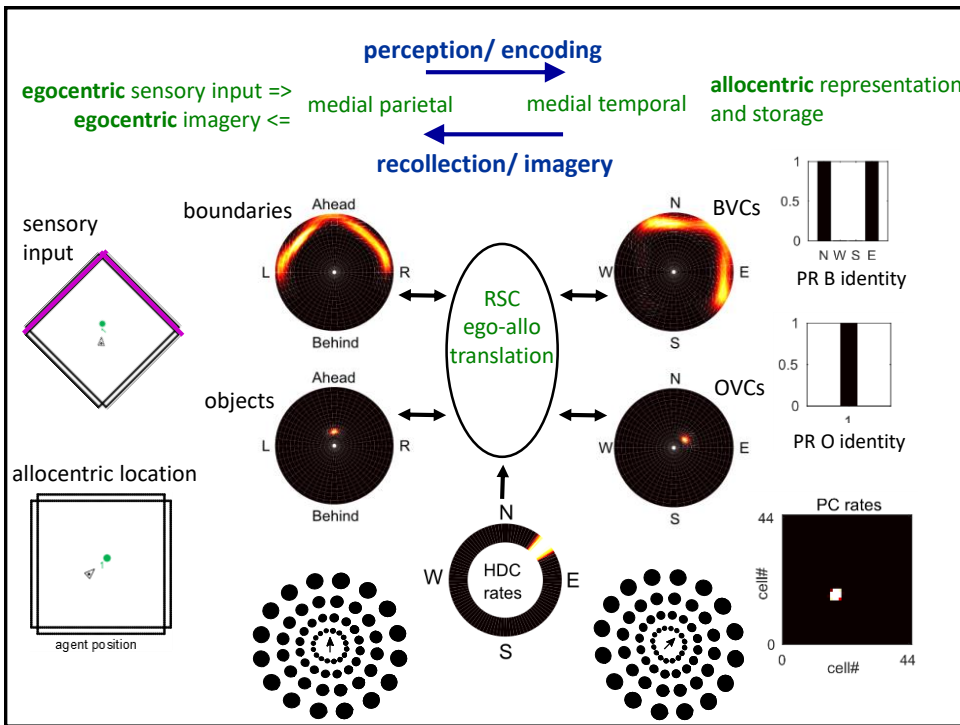
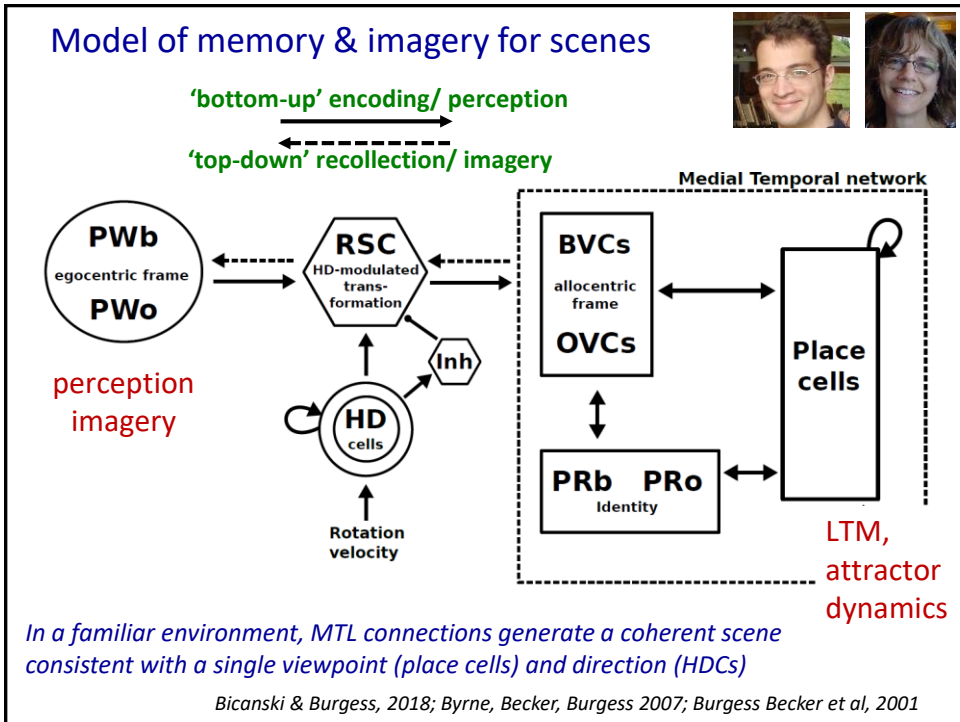
Similar responses seen in parieto-occipital ctx (Galletti et al., 1995)

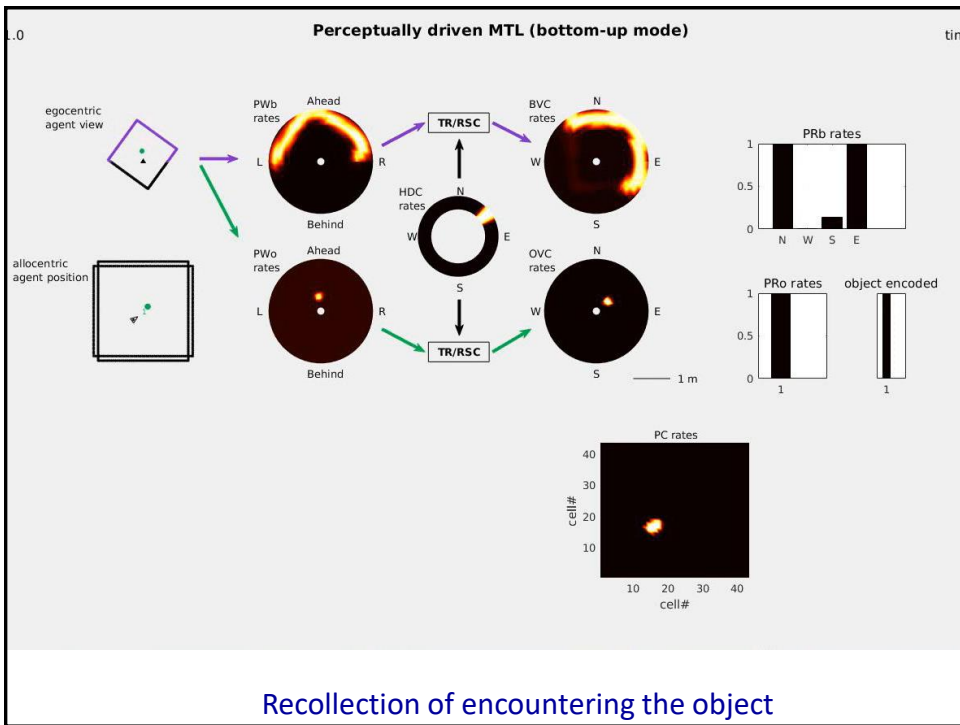
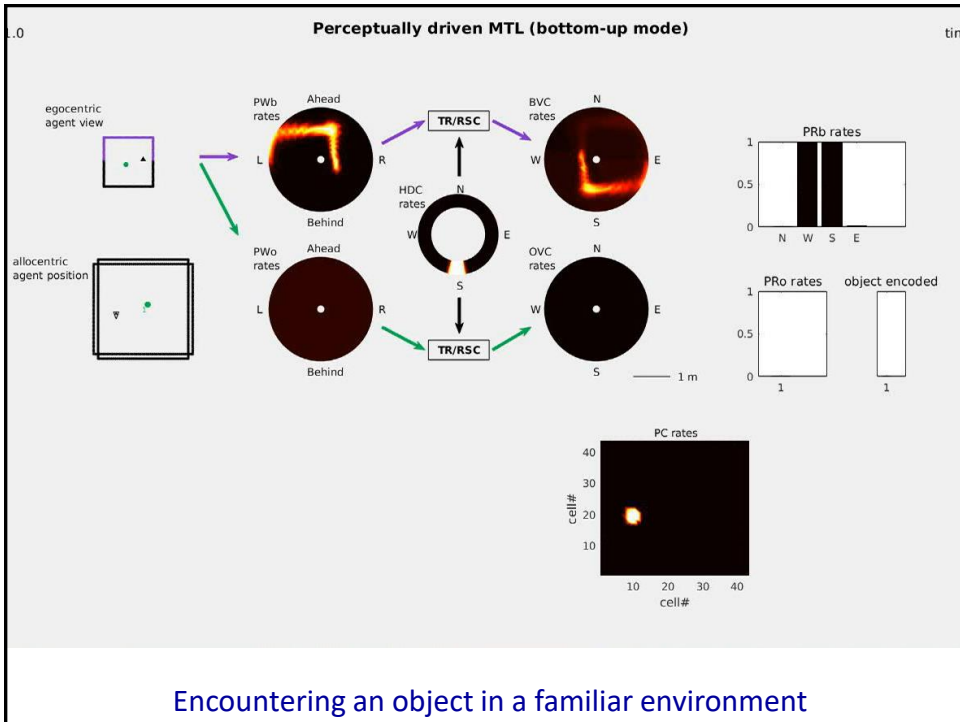


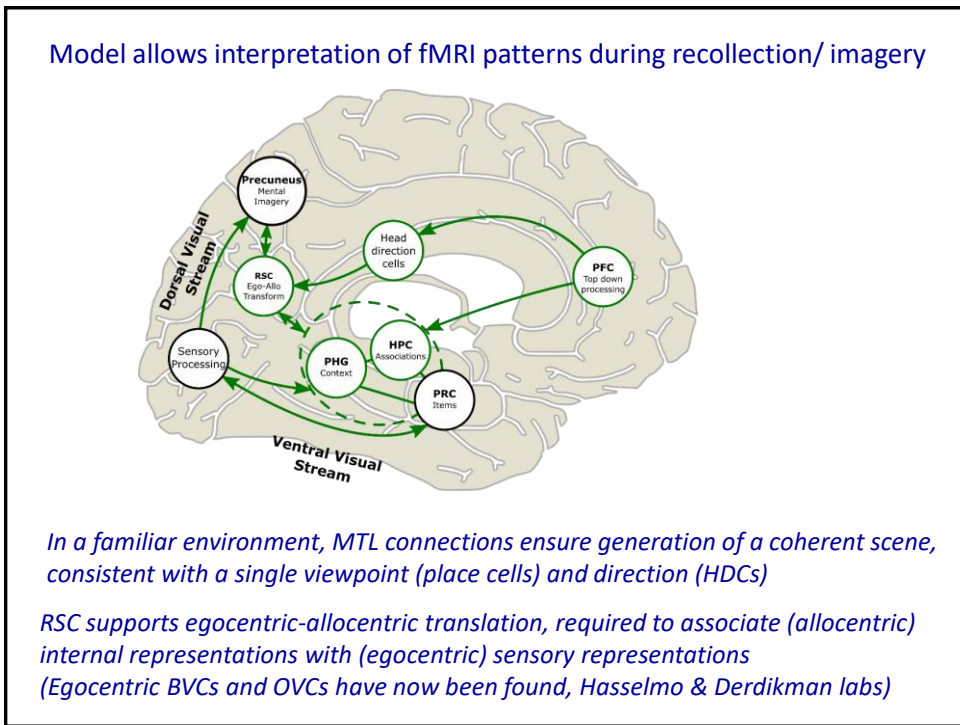
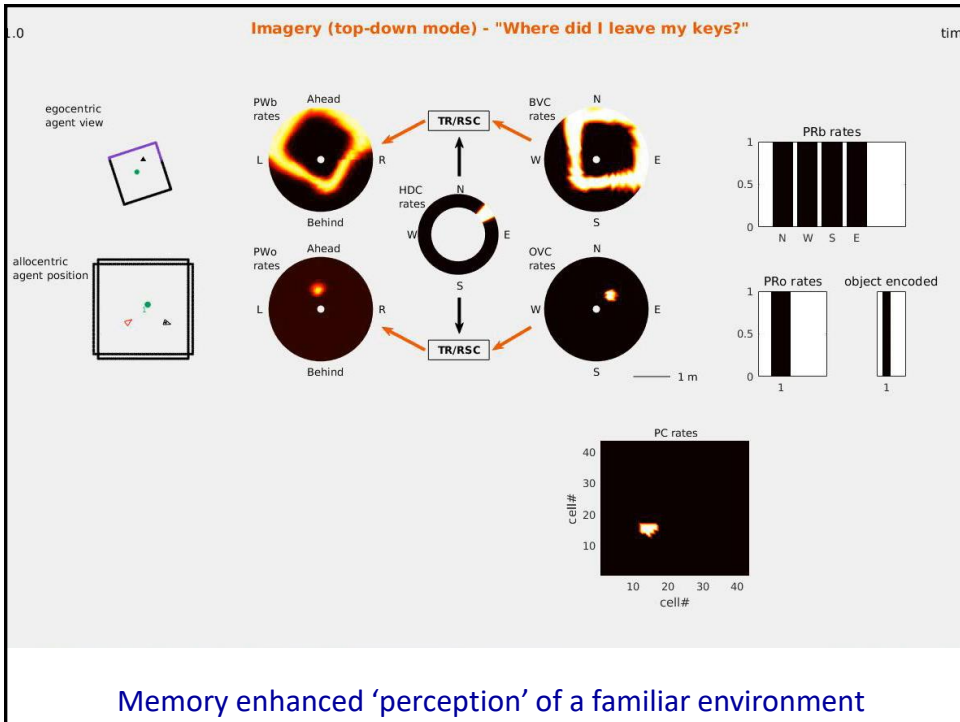




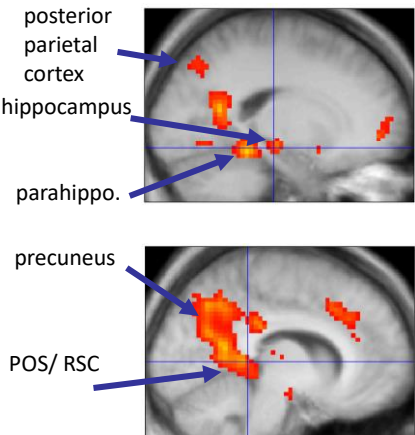
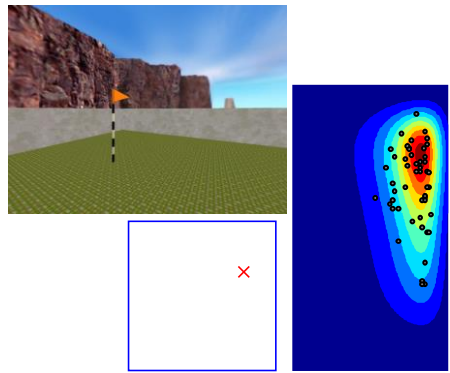








**Model allows interpretation of fMRI patterns during recollection/imagery & prediction of human search patterns**

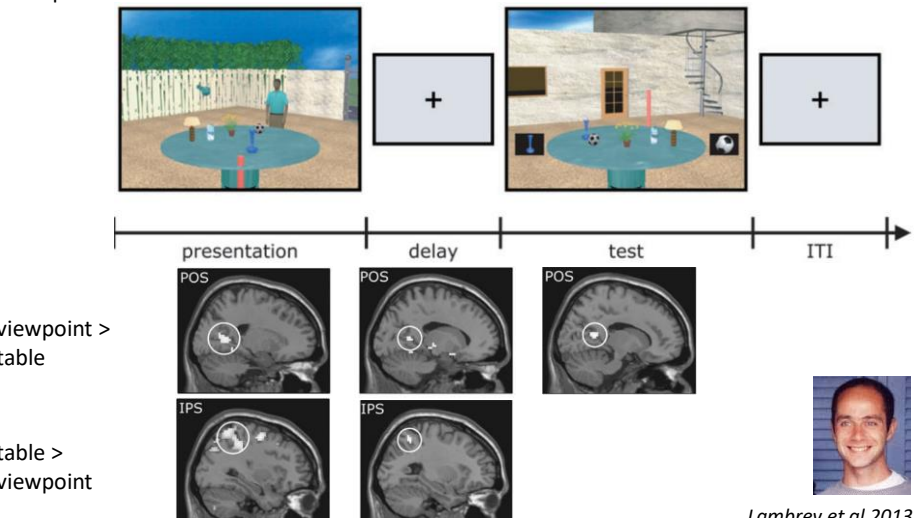
*Burgess et al, 2001* *Hartley et al, 2004*

**The network performs coherent spatial imagery, i.e. related to planning, 'episodic future thinking' and 'scene construction'**

*Addis and Schacter, 2007; Hassabis and Maguire, 2007*

**POS/ RSC activity and change of viewpoint in memory**

Viewpoint or table will rotate to avatar before test



viewpoint > table

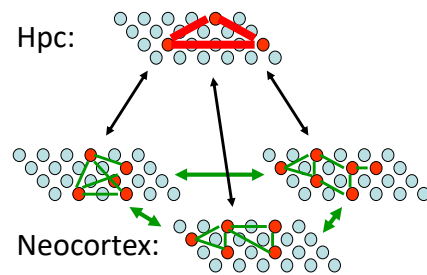
table > viewpoint

*Lambrey et al 2013*

**RSC associates internal (allocentric) representations to (egocentric) sensory inputs**  
 - strong associations form to stable sensory features (e.g. Auger et al., 2012)

## Relation to pattern completion and models of Episodic Memory

- Pattern completion is seen in reconstruction of location-object-identity in scene.
- Consistent with Marr's model of hippocampus & Tulving's idea of holistic episodic recollection/ re-experience.
- Consistent with measures of pattern completion in Episodic memory see Horner et al (2015).



**Marr, 1971;** Gardner-Medwin, McNaughton, Alvarez, Squire, McClelland, O'Reilly, Treves, Rolls, Teyler & DiScenna; Damasio;

## Functional roles for Papez's circuit?

Hippocampus (place cells):  
imposing a common viewpoint on retrieval/ imagery.

Fornix:

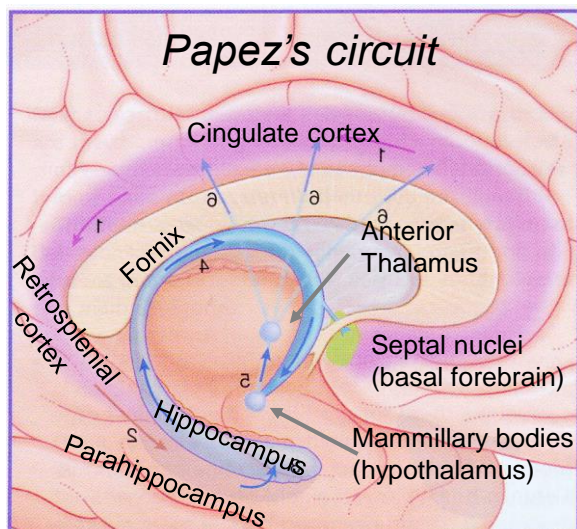
Head-direction cells: imposing a viewing direction

Theta cells/VCOs: grid cells, path integration, moving viewpoint in imagery.

ACh/novelty/learning

Diencephalic amnesia

(Aggleton & Brown, 1999; Gaffan; Delay & Brion 1969). E.g., patient NA (Squire & Slater, 1978), Korsakoff's syndrome.



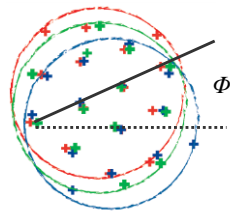
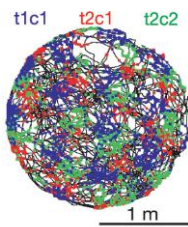


## Abstract neural representations

- 1) Frames of reference for spatial representation
- 2) Place cells & boundary vector cells
- 3) Neural level model of Spatial Memory and Imagery
- 4) **Place and grid cells, environmental and self-motion inputs?**
- 5) Grid cells as dynamic imagery?
- 6) Place and grid cells, representing states and transitions for planning?

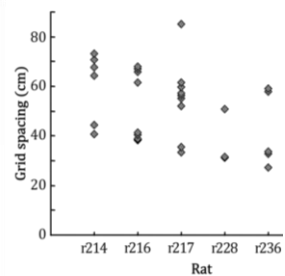
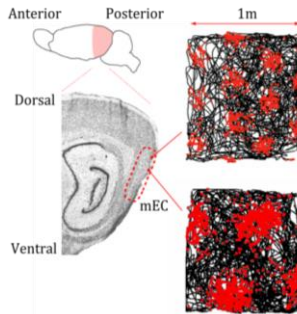
## Grid cells – thought to represent location by integrating self-motion.

The grids of nearby cells share orientation & scale

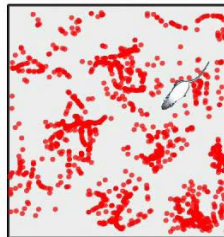


Hafting et al., 2005

Grid cells occur in modules with discrete scales



Barry et al, 2007;  
see also Stensola et al., 2012

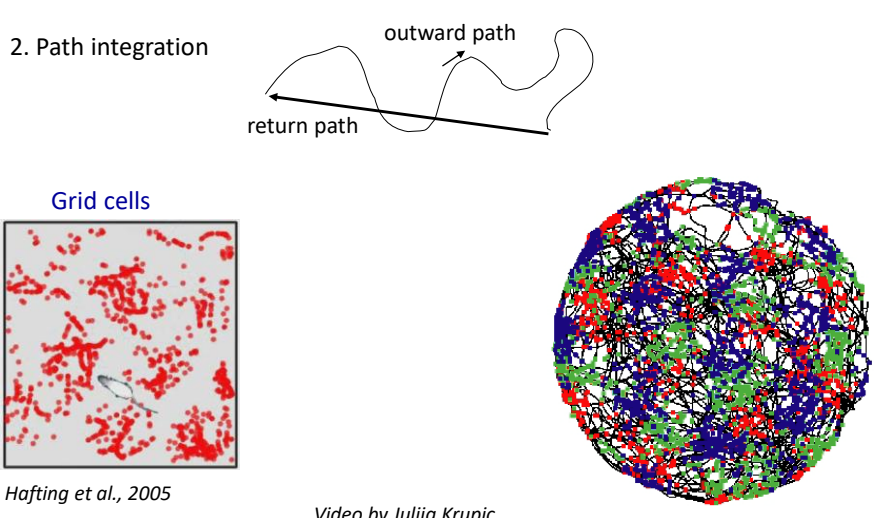


Video by Julija Krupic

**Two ways to know where you are:**

1. Environmental information  
(Environmental boundaries particularly influence place cells)
2. Path integration

**Grid cells**

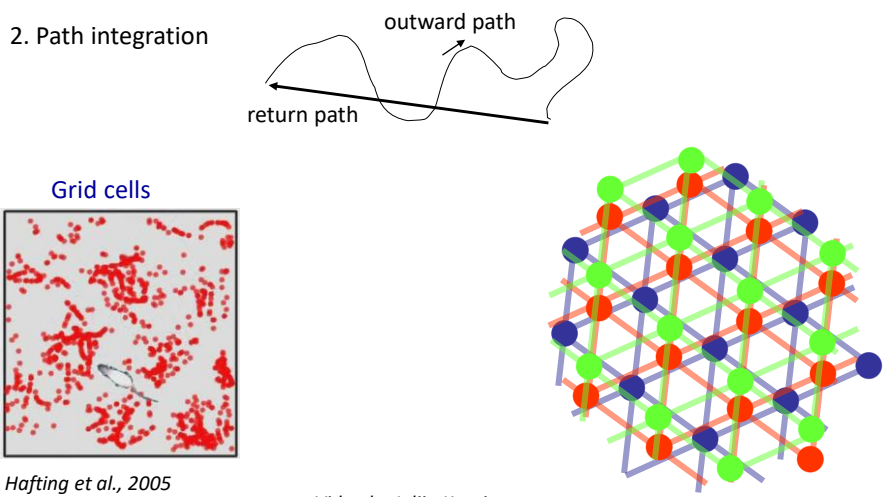


*Hafting et al., 2005* *Video by Julija Krupic*

**Two ways to know where you are:**

1. Environmental information  
(Environmental boundaries particularly influence place cells)
2. Path integration

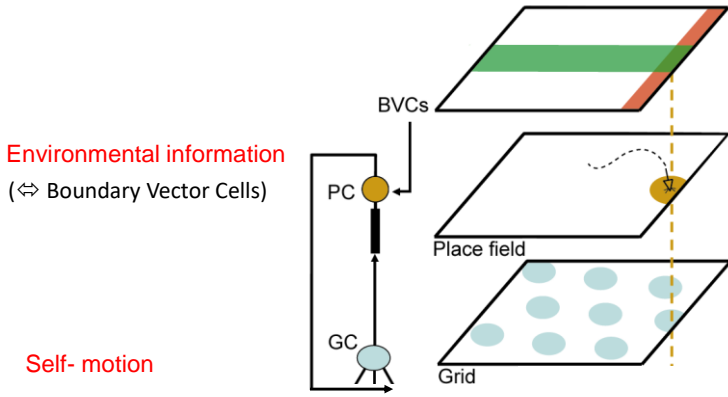
**Grid cells**



*Hafting et al., 2005* *Video by Julija Krupic*

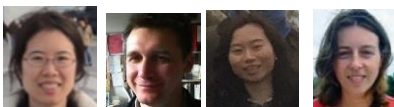
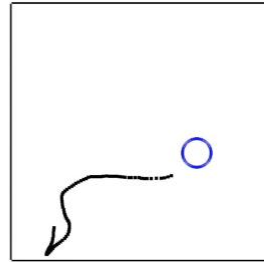
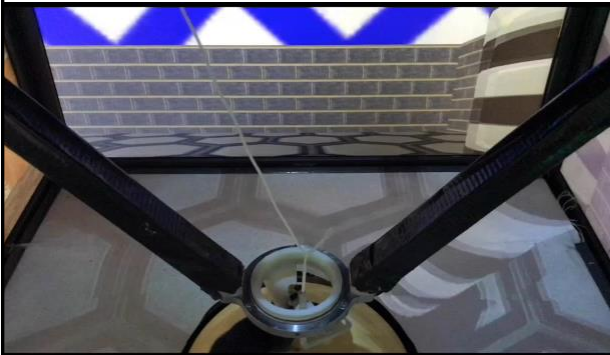
### Interactions between place cells and grid cells

Estimating self-location combines environmental & self-motion information

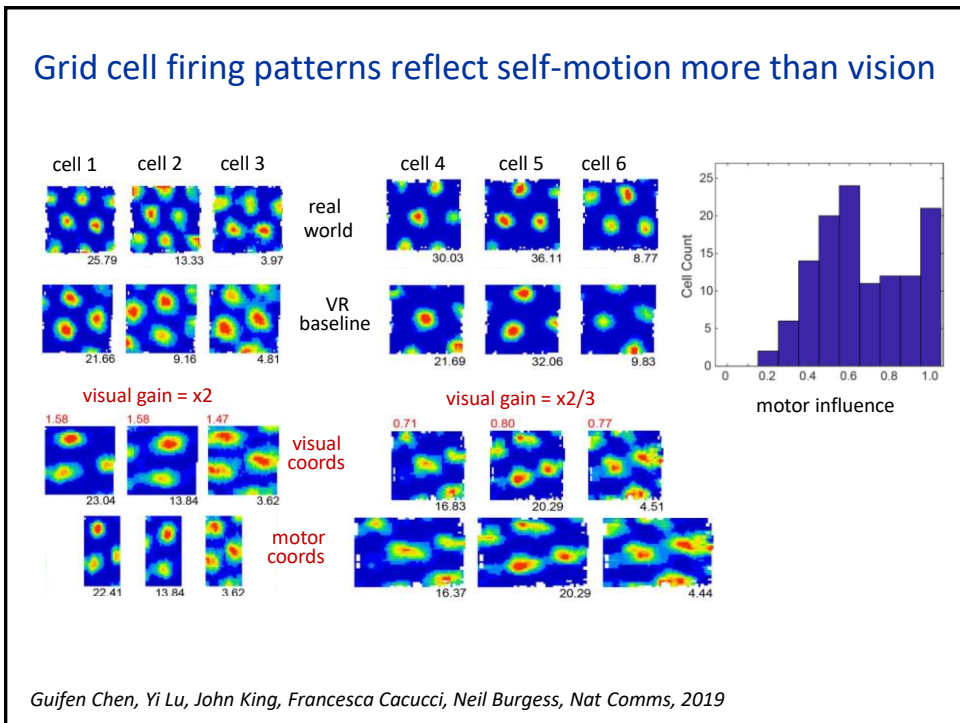
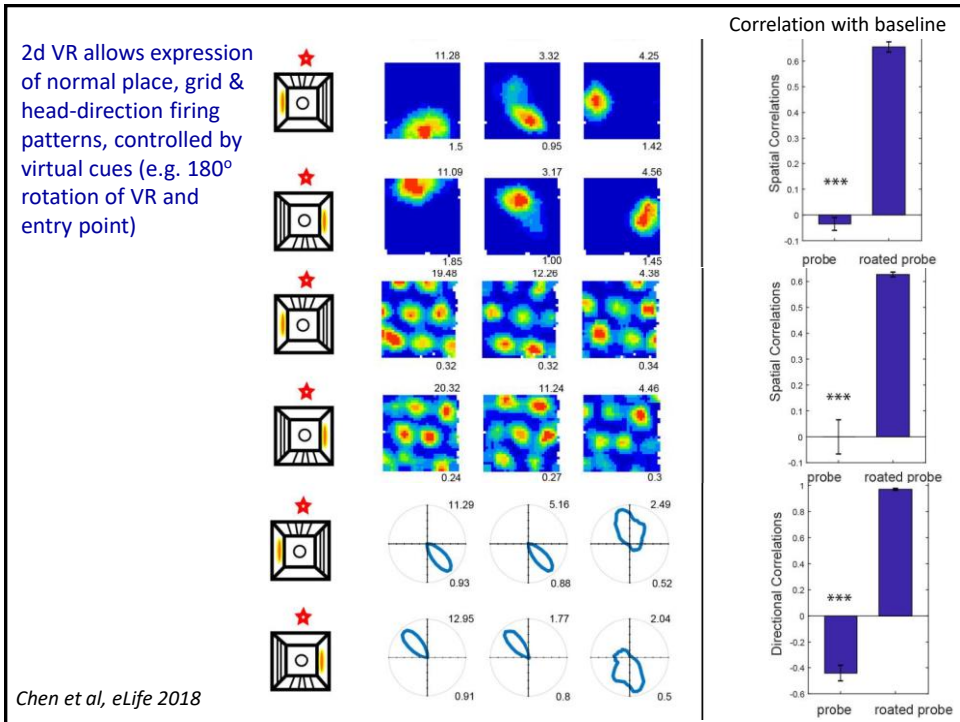


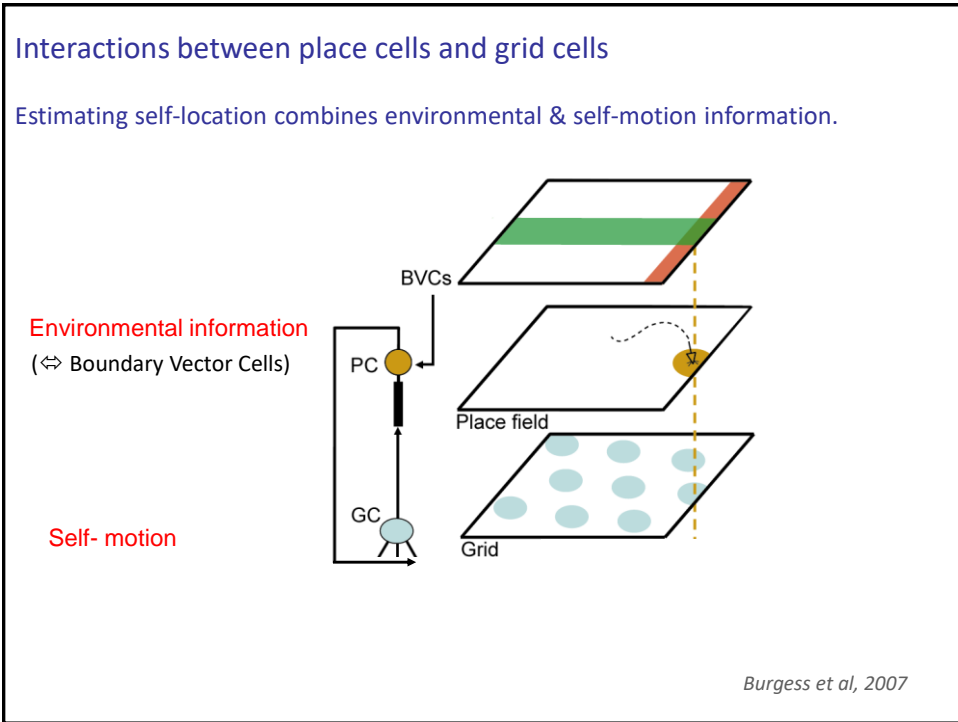
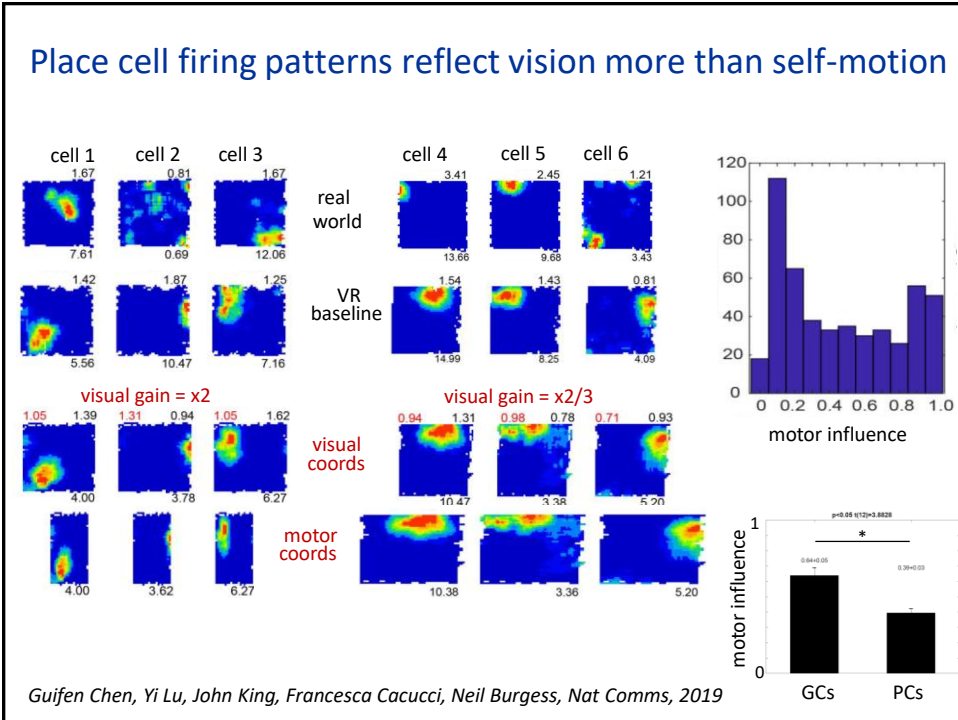
Burgess et al, 2007

### 2D VR for mice (invisible reward task)



Guifen Chen, John King, Yi Lu, Francesca Cacucci, Neil Burgess, eLife 2018

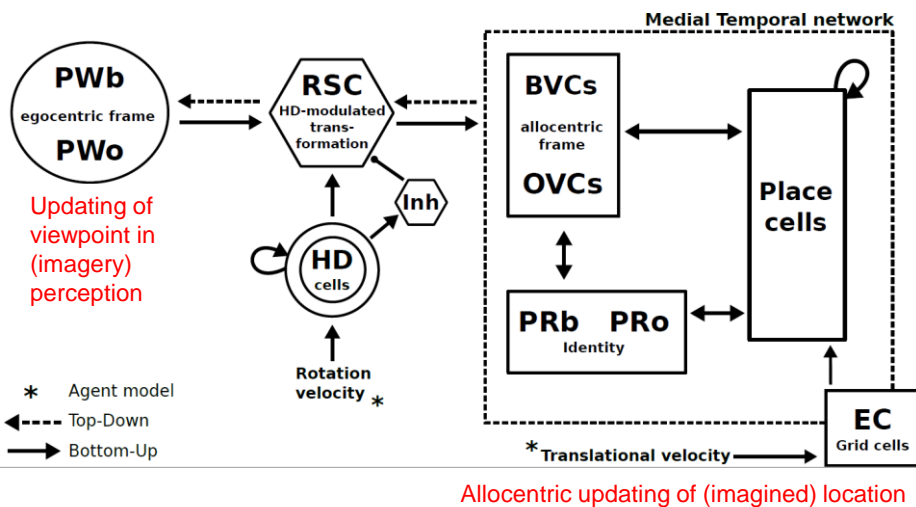




### Abstract neural representations

- 1) Frames of reference for spatial representation
- 2) Place cells & boundary vector cells
- 3) Neural level model of Spatial Memory and Imagery
- 4) Place and grid cells, environmental and self-motion inputs?
- 5) **Grid cells as dynamic imagery?**
- 6) Place and grid cells, representing states and transitions for planning?



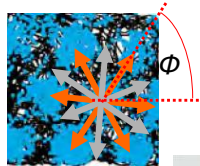
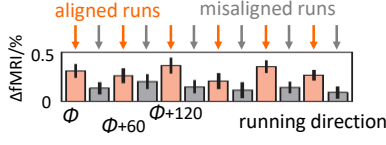

### Grid cells and memory/imagery



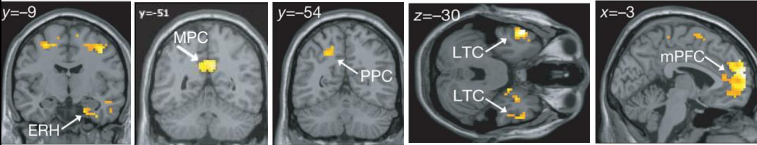

Bicanski & Burgess, eLife, 2018

### Grid cells in the human autobiographical memory system? Doeller, Barry, Burgess, 2010

populations of *aligned* grids (modules) => changes in fMRI signal with virtual running direction

Task designed by John King

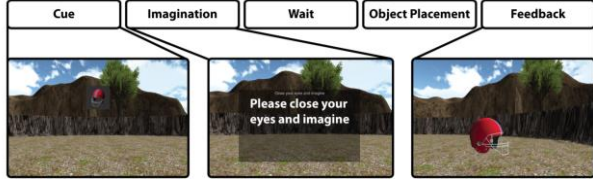
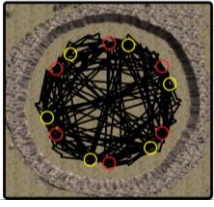



Autobiographical memory system

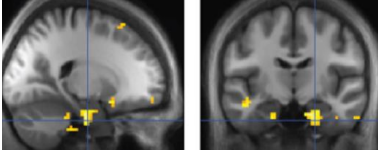
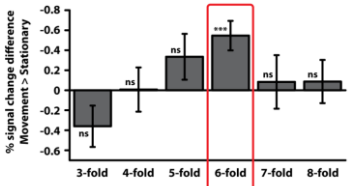
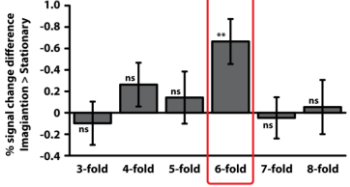
=> Grid cells allow path integration, and movement of viewpoint in imagery?

### Grid-like processing of movement of viewpoint in imagery


7.6secs	10.0secs	3.5secs	6.3secs	3.5secs
Cue	Imagination	Wait	Object Placement	Feedback

60° symmetry in fMRI signal with *imagined* running direction in Entorhinal cortex (aligned with that in virtual movement)

Horner et al., 2016



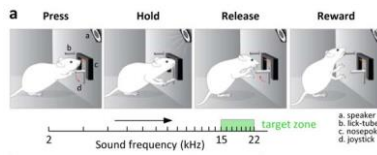
### Abstract neural representations

- 1) Frames of reference for spatial representation
- 2) Place cells & boundary vector cells
- 3) Neural level model of Spatial Memory and Imagery
- 4) Place and grid cells, environmental and self-motion inputs?
- 5) **Grid cells as dynamic imagery?**
- 6) Place and grid cells, representing states and transitions for planning?

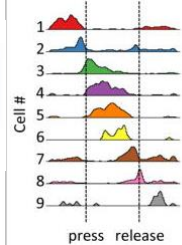
Hippocampal cells can represent abstract concepts, such as 'place' but also, e.g., personal identity or sound frequency?



Quiroga et al., (2005)

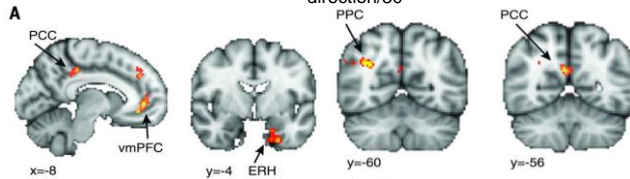


Aronov, Nevers, Tank (2017)



Grid cell firing patterns reflect the transition structure of learned conceptual spaces?

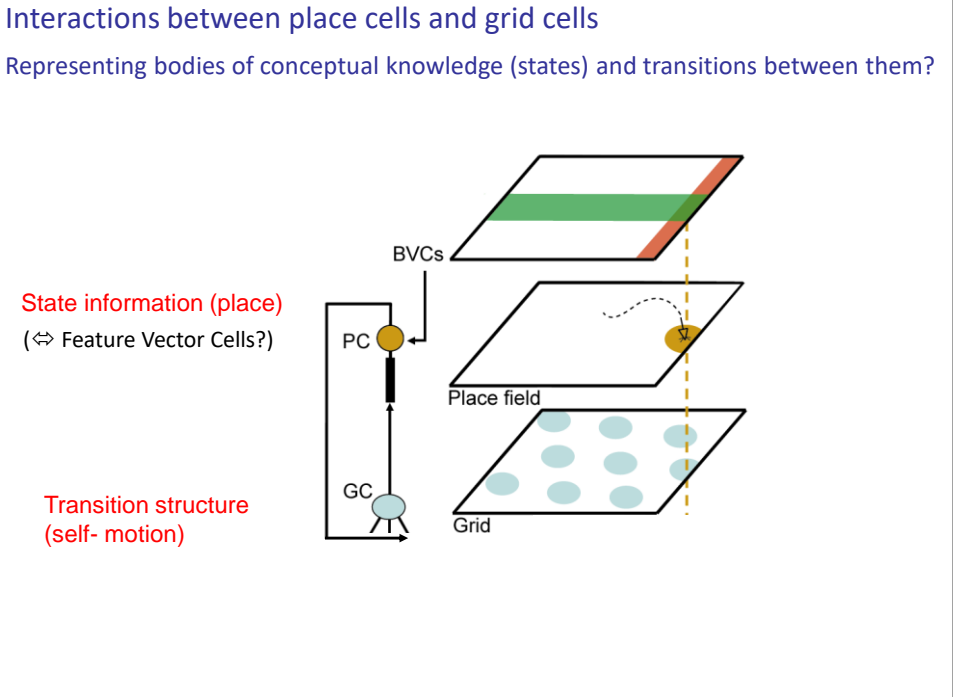
Navigation in space of bird neck & leg length



Constantinescu, O'Reilly, Behrens 2016







### 'Intuitive Planning..'

States  $x_i$

Transition matrix ( $T$ )

probability of transition from state 2 to state 3 in one step

probability of transition from state 11 to state 8 in one step

States

..with neural populations

PC<sub>i</sub> firing profile is  $E_i$   
firing rate is  $f_i(x(t))$ :  $E_i$  (peak at  $x_i$ )

PC<sub>k</sub> firing profile is  $E_k$  (peak at  $x_k$ )

$P(x(t))$  is a vector over states  $x_i$ :  
 $P(x(t)) \sim \sum_j f_j(x(t)) E_j$   
 $P(x(t+1)) \sim \sum_j f_j(x(t)) T E_j$

PC population

GC<sub>i</sub> firing profile is  $G_i$   
firing rate =  $g_i(x(t))$ :  $G_i$

$P(x(t)) \sim \sum_j g_j(x(t)) G_j$   
 $P(x(t+1)) \sim \sum_j g_j(x(t)) T G_j$

If  $T G_j(x) = \lambda_j G_j(x)$   
 $P(x(t+1)) \sim \sum_j \lambda_j g_j(x(t)) G_j$

$P(x(\tau \geq t) | x(t))$   
 $\sim \sum_j (\gamma \lambda_j + \gamma^2 \lambda_j^2 + \dots) g_j(x(t)) G_j$   
 $\sim \sum_j g_j(x(t)) G_j / (1 - \gamma \lambda_j)$

$P(x(t))$  is a vector over states  $x_i$

$P(x(t+1)) = T P(x(t))$

$P(x(t+2)) = T^2 P(x(t))$

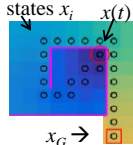
$P(x(t+3)) = T^3 P(x(t))$

States  $x_i$

Stachenfeld, Botvinick, Gershman, Gerstner, Baram., Behrens

**..with neural populations**

$P(x(\tau \geq t) = x_G | x(t))$   
 $\sim \sum_j g_j(x(t)) G_j(x_G) / (1 - \gamma \lambda_j)$   
 the discounted future prob.  
 of reaching  $x_G$  from  $x(t)$ ,  
 a.k.a the 'successor  
 representation'  $\mathbf{M}(x(t), x_G)$



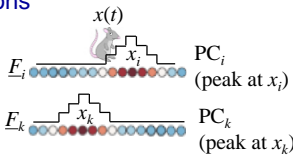
states  $x_i$   $x(t)$   
 $x_G \rightarrow$

**E.g. place cell read-out of GCs**

PC<sub>i</sub> firing rate  $f_i(x(t))$ , driven by GCs,  
 could approx. current or future  
 occupancy of state  $x_i$

$P(x(t) = x_i) \sim f_i(x(t)) = \sum_j w_{ij} g_j(x(t))$   
 [e.g. Hebbian  $w_{ij} \sim \underline{E}_i \cdot \underline{G}_j$ ]. Then  
 $P(x(t+1) = x_i) \sim \sum_j \lambda_j w_{ij} g_j(x(t))$   
 $P(x(\tau \geq t) = x_i) \sim \sum_j w_{ij} g_j(x(t)) / (1 - \gamma \lambda_j)$

PC<sub>i</sub> firing profile is  $\underline{E}_i$   
 firing rate is  $f_i(x(t))$ :

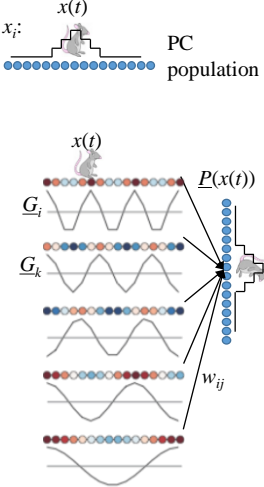


PC<sub>i</sub> (peak at  $x_i$ )  
 PC<sub>k</sub> (peak at  $x_k$ )

$\underline{P}(x(t))$  is a vector over states  $x_i$ :

$\underline{P}(x(t)) \sim \sum_j f_j(x(t)) \underline{E}_j$   
 $\underline{P}(x(t+1)) \sim \sum_j f_j(x(t)) \mathbf{T} \underline{E}_j$

GC<sub>i</sub> firing profile is  $\underline{G}_i$   
 firing rate =  $g_i(x(t))$ :

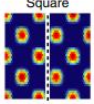


$\underline{P}(x(t)) \sim \sum_j g_j(x(t)) \underline{G}_j$   
 $\underline{P}(x(t+1)) \sim \sum_j g_j(x(t)) \mathbf{T} \underline{G}_j$   
 If  $\mathbf{T} \underline{G}_j(x) = \lambda_j \underline{G}_j(x)$   
 $\underline{P}(x(t+1)) \sim \sum_j \lambda_j g_j(x(t)) \underline{G}_j$   
 $\underline{P}(x(\tau \geq t) | x(t))$   
 $\sim \sum_j (\gamma \lambda_j + \gamma^2 \lambda_j^2 + \dots) g_j(x(t)) \underline{G}_j$   
 $\sim \sum_j g_j(x(t)) \underline{G}_j / (1 - \gamma \lambda_j)$

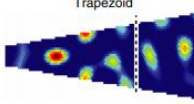
*Stachenfeld, Botvinick, Gershman, Gerstner, Baram.. Behrens*

**Using Eigenvectors of the task Transition Matrix as basis vectors to represent state occupancy makes prediction easy.**

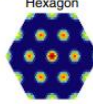
.. and Grid firing profiles might be Eigenvectors of a *diffusive* transition matrix  $\mathbf{T}$   
 (i.e.  $\mathbf{T} \underline{G}_i(x) = \lambda_i \underline{G}_i(x)$ ), or of the *covariance* matrix of PC firing (e.g. learned via Oja's rule)



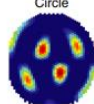
Square



SR eigenvector grid fields  
Trapezoid

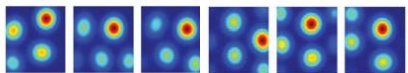


Hexagon



Circle

*(Stachenfeld et al., 2017)*



*(Dordek et al., 2015)*

**Implications**

- Place cell read-out shifts from current to future locations by re-weighting Grid cell inputs, and can give 'Successor Representation' i.e.  $P(x(\tau \geq t) = x_i | x(t))$
- Successor Representation allows navigation to any other state (via gradient ascent)
- Common transition structure across tasks captured by GCs, while PCs reflect specific sensory input & 'remap', allows generalisation by separating structure from content, (*Whittington et al Cell, 2020*)

### Conclusions

- Considerable progress has been made in understanding how environmental and self-motion information combine in neural representations of location and orientation in rodents.
- We can use this to create a neural-level understanding of spatial memory, learning and imagination in humans, and begin to apply it to conceptual knowledge?

#### Thanks to:

*Andrej Bičanski*  
*John King*  
*Guifen Chen*  
*Yi Lu*  
*John O'Keefe*  
*Francesca Cacucci*  
*Tim Behrens*

*Dan Bush*  
*Caswell Barry*  
*Christian Doeller*  
*Colin Lever*  
*Suzanna Becker*  
*Tom Hartley*  
*Hugo Spiers*

