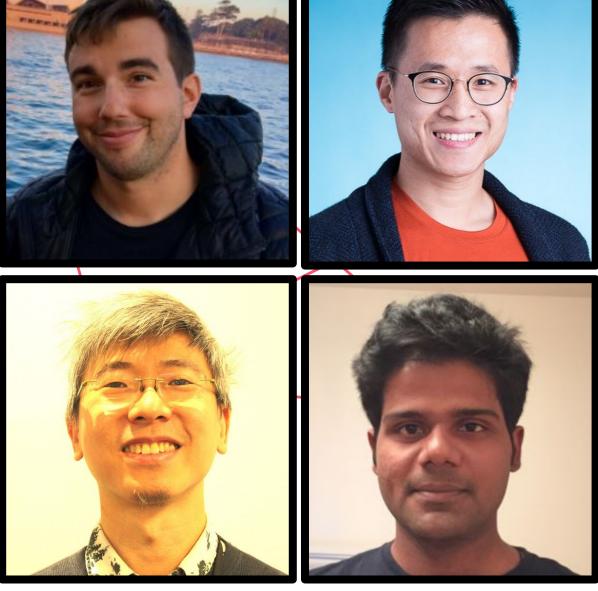


Detecting Out-of-Distribution Inputs to Deep Generative Models Using Typicality

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Deep Generative Models and Out-of-Distribution Inputs Motivation

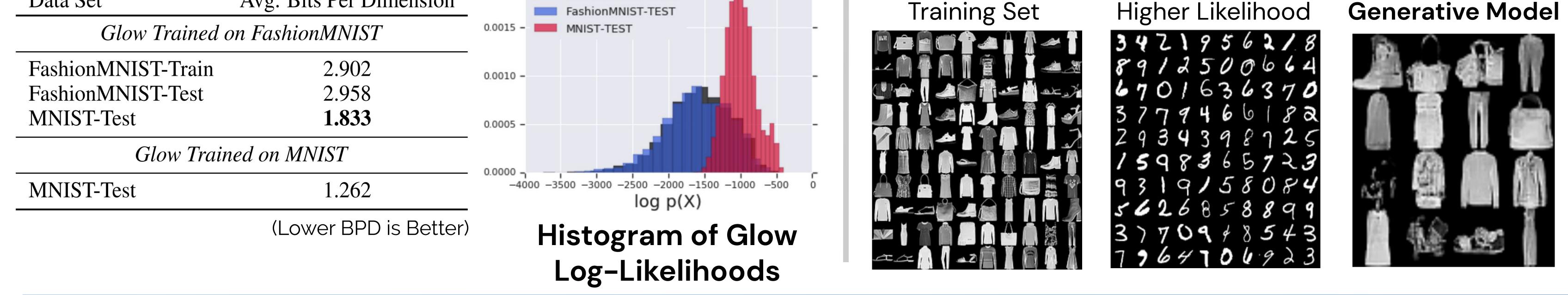
Nalisnick et al. [ICLR 2019] showed that the likelihood of deep generative models cannot distinguish the training data from out-of-distribution (OOD) inputs.

Yet when we sample from the generative model, the outputs conspicuously resemble the training data, not the OOD inputs.

FashionMNIST:

MNIST:

Samples from

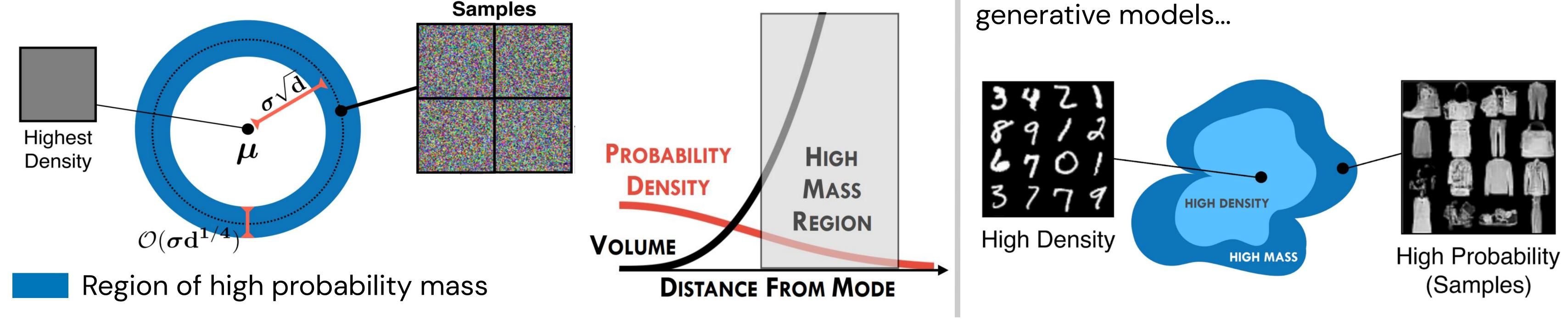


Background Concentration and Typicality

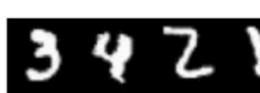
Consider a high-dimensional Gaussian centered on the all-gray image...

Avg. Bits Per Dimension

Data Set



We conjecture that a similar phenomenon is happening with high-dimensional deep generative models...







A Goodness-of-Fit Test for OOD Detection Methodology

Due to deep generative models having an intractable cumulative distribution function (CDF), we propose detecting OOD inputs via a hypothesis based off of Shannon's [1948] definition of typical sets.

0.6 -

0.4 -

of Batches

Fraction

Definition 2.1. ϵ -Typical Set [11] For a distribution $p(\mathbf{x})$ with support $\mathbf{x} \in \mathcal{X}$, the ϵ -typical set $\mathcal{A}_{\epsilon}^{N}[p(\mathbf{x})] \in \mathcal{X}^{N}$ is comprised of all N-length sequences that satisfy

$$\mathbb{H}[p(\mathbf{x})] - \epsilon \leq \frac{-1}{N} \sum_{n=1}^{N} \log p(\boldsymbol{x}_n) \leq \mathbb{H}[p(\mathbf{x})] + \epsilon$$

where $\mathbb{H}[p(\mathbf{x})] = \int_{\mathcal{X}} p(\mathbf{x})[-\log p(\mathbf{x})]d\mathbf{x}$ and $\epsilon \in \mathbb{R}^+$ is a small constant.

Algorithm 1 A Bootstrap Test for Typicality

Input: Training data X, validation data X', trained model $p(\mathbf{x}; \boldsymbol{\theta})$, number of bootstrap samples K, significance level α , M-sized batch of possibly OOD inputs X.

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Offline prior to deployment
1. Compute \hat{\mathbb{H}}^{N}[p(\mathbf{x}; \boldsymbol{\theta})] = \frac{-1}{N} \sum_{n=1}^{N} \log p(\boldsymbol{x}_{n}; \boldsymbol{\theta}).
2. Sample K M-sized data sets from \mathbf{X}' using bootstrap resampling.
3. For all k \in [1, K]:
        Compute \hat{\epsilon}_k = \left| \frac{-1}{M} \sum_{m=1}^{M} \log p(\boldsymbol{x}'_{k,m}; \boldsymbol{\theta}) - \hat{\mathbb{H}}^N[p(\mathbf{x}; \boldsymbol{\theta})] \right| (Equation 7)
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For an *M*-sized test batch $\widetilde{\boldsymbol{X}} = \{ \widetilde{\boldsymbol{x}}_1, \dots, \widetilde{\boldsymbol{x}}_M \}$ $\texttt{if } \widetilde{\boldsymbol{X}} \in \mathcal{A}_{\epsilon}^{M}[p(\mathbf{x}; \boldsymbol{\theta})] \texttt{ then } \widetilde{\boldsymbol{X}} \sim p(\mathbf{x}; \boldsymbol{\theta}), \texttt{ otherwise } \widetilde{\boldsymbol{X}} \not \sim p(\mathbf{x}; \boldsymbol{\theta})$ Experiment **Fraction of M-Sized Batches** Classified as OOD (α =99%) 0.0020 000 8 1.0 as ID: FashionMNIST-TEST **ID: FashionMNIST-TEST** g Classified a

OOD: MNIST-TEST

80

Batch Size (M)

60

40

4. Set $\epsilon_{\alpha}^{M} = \text{quantile}(F(\epsilon), \alpha)$ (e.g. $\alpha = .99$)

Online during deployment $\mathbf{If} \left| \frac{-1}{M} \sum_{m=1}^{M} \log p(\tilde{\boldsymbol{x}}_m) - \mathbb{\hat{H}}^N[p(\mathbf{x}; \boldsymbol{\theta})] \right| > \epsilon_{\alpha}^M:$ **Return** $\widetilde{\mathbf{X}}$ is out-of-distribution Else: Return $\widetilde{\mathbf{X}}$ is in-distribution

OOD: NotMNIST-TEST

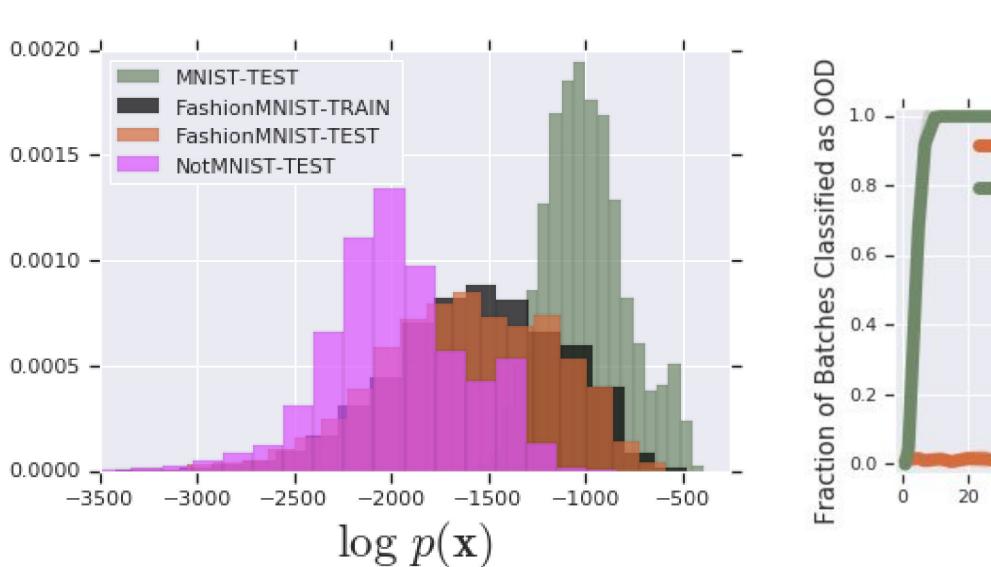
100

Batch Size (M)

- Our test for typicality **detects many** of the OOD sets found problematic in Nalisnick et al. [ICLR 2019].
- Relies on the distribution of model likelihoods being well separated.

• ArXiv Link:

https://arxiv.org/abs/1906.02994



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