Introduction to Neural Coding

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The CNS



Neocortex



Cortical layers



В



Neural signals (in vivo)

Aggregate

- aggregate fields EEG, MEG, LFP
- aggregate membrane voltage die imaging
- metabolism fMRI, PET, intrinsic imaging

Single neuron

- extracellular single neuron, spike sorting, cell attach
- intracellular sharp electrode, whole cell

Senses

How many senses do you have?

- taste (gustation)
- smell (olfaction)
- hearing (audition)
- sight (vision)
- touch (somatosensation)
- pain (nociception)
- body configuration (proprioception)
- acceleration and balance (vestibular sense)

Neocortical senses



Sensory areas



Common features of neocortical senses

- common pathways: receptors subctx nuclei thalamus primary ctx higher ctx
- thalamic loops between cortical areas
- feedback
- parallel hierarchy
- alternate pathways tectal, para-lemniscal

Common processing

- receptor discretisation sampling
- receptive fields
- contrast sensitivity Weber's law
- adaptation
 - neural vs. psychological
 - adaptation to higher features
 - mismatch negativity
 - statistical adaptation

Quantifying responses

- receptive fieds
- motor fields
- stimulus-response functions
- sensory computation and encoded variables
- tuning curves

Optimality of coding

- "impedence" matching between different components
- matching to natural statistics
- matching to behaviourally relevant features
- redundancy reduction

The eye and retina





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Centre-surround receptive fields



Colour at the retina



В

Centre-surround models

Centre-surround receptive fields are commonly described by one of two equations, giving the scaled response to a point of light shone at the retinal location (x, y).

A difference-of-Gaussians (DoG) model:

$$D_{\text{DoG}}(x,y) = \frac{1}{2\pi\sigma_c^2} \exp\left(-\frac{(x-c_x)^2 + (y-c_y)^2}{2\sigma_c^2}\right) - \frac{1}{2\pi\sigma_s^2} \exp\left(-\frac{(x-c_x)^2 + (y-c_y)^2}{2\sigma_s^2}\right)$$

Centre-surround models

... or a Laplacian-of-Gaussian (LoG) model:



Linear receptive fields

The linear-like response apparent in the prototypical experiments can be generalised to give a predicted firing rate in response to an arbitrary stimulus s(x, y):

$$r(s(x,y)) = \int dx \, dy \, D(x,y) s(x,y)$$

The receptive field centres (c_x, c_y) are distributed over visual space. If we let D() represent the RF function centred at 0, instead of at (c_x, c_y) , we can write:

$$r(c_x, c_y; s(x, y)) = \int dx \, dy \, D(c_x - x, c_y - y) s(x, y)$$

which looks like a convolution.

Frequency effects

Thus a repeated linear receptive field acts like a spatial filter. We can consider its frequency response.

Both DoG and LoG models are bandpass. Taking 1D versions:



Edge detection

Bandpass filters emphasise edges:



orginal image



DoG responses



thresholded

Thalamic relay



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Visual cortex



Orientation selectivity



Linear receptive fields – simple cells

Linear response encoding:

$$r(t_0, s(x, y, t)) = \int_0^\infty d\tau \int dx \, dy \, s(x, y, t_0 - \tau) D(x, y, \tau)$$

For separable receptive fields:

$$D(x, y, \tau) = D_s(x, y)D_t(\tau)$$

For simple cells:

$$D_{s} = \exp\left(-\frac{(x-c_{x})^{2}}{2\sigma_{x}^{2}} - \frac{(y-c_{y})^{2}}{2\sigma_{y}^{2}}\right)\cos(kx-\phi)$$

Linear response functions – simple cells



Simple cell orientation selectivity



 ${\mathcal X}$

Drifting gratings



$$s(x, y, t) = G + A\cos(kx - \phi)\cos(\omega t)$$

Separable and inseparable response functions



Separable: motion sensitive; not direction sensitive Inseparable: motion sensitive; and direction sensitive

Complex cells

Complex cells are sensitive to orientation, but, supposedly, not phase.

One model might be (neglecting time)

$$\begin{aligned} r(s(x,y)) &= \left[\int dx \ dy \ s(x,y) \exp\left(-\frac{(x-c_x)^2}{2\sigma_x^2} - \frac{(y-c_y)^2}{2\sigma_y^2}\right) \cos(kx)\right]^2 \\ &+ \left[\int dx \ dy \ s(x,y) \exp\left(-\frac{(x-c_x)^2}{2\sigma_x^2} - \frac{(y-c_y)^2}{2\sigma_y^2}\right) \cos(kx-\pi/2)\right]^2 \end{aligned}$$

But many cells do have some residual phase sensitivity. Quantified by $(f_1/f_0$ ratio).

Stimulus-response functions (and constructive models) for complex cells are still a matter of debate.

Other V1 responses

- end-stopping
- blobs and colour
- surround effects
- . . .

Higher Visual Areas

