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Optimal indolence: a normative microscopic approach to work and leisure

Ritwik K. Niyogi1, Yannick-Andre Breton2, Rebecca B. Solomon2, Kent Conover2, Peter Shizgal2 and Peter Dayan1

1Gatsby Computational Neuroscience Unit, University College London, London, UK
2Center for Studies in Behavioral Neurobiology, Concordia University, Montreal, Quebec, Canada

Dividing limited time between work and leisure when both have their attractions is a common everyday decision. We provide a normative control-theoretic treatment of this decision that bridges economic and psychological accounts. We show how our framework applies to free-operant behavioural experiments in which subjects are required to work (depressing a lever) for sufficient total time (called the price) to receive a reward. When the microscopic benefit-of-leisure increases nonlinearly with duration, the model generates behaviour that qualitatively matches various microfeatures of subjects’ choices, including the distribution of leisure bout durations as a function of the payoff. We relate our model to traditional accounts by deriving macroscopic, molar, quantities from microscopic choices.

1. Introduction

What to do, when to do it and how long to do it for are fundamental questions for behaviour. Different options across these dimensions of choice yield different costs and benefits, making for a rich, complex, optimization problem.

One common decision is between working (performing an employer-defined task) and engaging in leisure (activities pursued for oneself). Working leads to external rewards, such as food and money; whereas leisure is supposed to be intrinsically beneficial (otherwise, one would not want to engage in it). As these activities are usually mutually exclusive, subjects must decide how to allocate time to each. Note that work need not be physically or cognitively demanding, but consumes time; equally leisure need not be limited to rest and may present physical and/or mental demands.

This decision has been studied by economists [1–5], behavioural psychologists [6–16], ethologists [17] and neuroscientists [18–24]. Tasks involving free-operant behaviour are particularly revealing, because subjects can choose what, when and how, minimally encumbered by direct experimenter intervention. We consider the cumulative handling time (CHT) schedule brain stimulation reward (BSR) paradigm of Shizgal and co-workers [20,21], in which animals have to invest quantifiable work to get rewards that are psychophysically stationary and repeatable.

Most previous investigations of time allocation (TA) have focused on molar or macroscopic characterizations of behaviour [1,2,4,10,18,21–23,25–31], capturing the average times allocated to work or leisure. Here, we characterize the detailed temporal topography of choice, i.e. the fine-scale molecular or microscopic structure of allocation [32–37], that is lost in molar averages (figure 1c). We build an approximately normative, reinforcement-learning, account, in which microscopic choices approximately maximize net benefit. Our central intent is to understand the qualitative structure of the molecular behaviour of subjects, providing an account that can generalize to many experimental paradigms. Therefore, although we apply the model to a set of CHT experiments in rats it is the next stage of the programme to fit this behaviour quantitatively in detail.

Having introduced previous approaches, we describe an example task and experiments (§2), key molecular features of the data from those (§3), our novel normative, microscopic approach (§4) and how it captures these key features (§5).
2. Task and experiment

As an example paradigm employed in rodents, consider a CHT task [20,21] in which subjects choose between working—the facile task of holding down a light lever—and engaging in leisure, i.e. resting, grooming, exploring, etc. (figure 1a). A BSR [38] is given after the subject has accumulated work for an experimenter-defined total time-period called the price (P) in order to obtain a single reward (black dot) of subjective RI. The trial duration is 25 × price (plus 2 s each time the price is attained, during which the lever is retracted so it cannot work; not shown). The RI and price are held fixed within a trial. (b) Molar TA functions of a typical subject as a function of RI and price. Red/grey curves: effect of RI, for a fixed short price; blue/dark grey curves: effect of price, for a fixed high RI; green/light grey curves: joint effect of RI and price. (c) A molecular analysis may reveal different microstructures of working and engaging in leisure. The three rows show three different hypothetical trials. All three microstructures have the same molar TA, but are clearly distinguishable. (d) Molecular ethogram showing the detailed temporal topography of working and engaging in leisure for the subject in (b). Upper, middle and lower panels show low, medium and high pay-offs, respectively, for a fixed, short price. Following previous reports using rat subjects, releases shorter than 1 s are considered part of the previous work bout (as subjects remain at the lever during this period). Graphically, this makes some work bouts appear longer than the others. The subject mostly pre-commits to working continuously for the entire price duration. When the pay-off is high, the subject works almost continuously for the entire trial, engaging in very short leisure bouts inbetween work bouts. When the pay-off is low, the subject engages in a long leisure bout after receiving a reward. This leisure bout is potentially longer than the trial, whence it would be censored. The part of a trial before the reward, price and probability of reward delivery are certainly known is coloured pink/dark and not considered further. Data collected by Y.-A.B. and R.S. and initially reported in [38]. (Online version in colour.)

Figure 1. Task and key features of the data. (a) CHT task. Grey bars denote work (depressing a lever), white gaps show leisure. The subject must accumulate work up to a total period of time called the price (P) in order to obtain a single reward (black dot) of subjective RI. The trial duration is 25 × price (plus 2 s each time the price is attained, during which the lever is retracted so it cannot work; not shown). The RI and price are held fixed within a trial. (b) Molar TA functions of a typical subject as a function of RI and price. Red/grey curves: effect of RI, for a fixed short price; blue/dark grey curves: effect of price, for a fixed high RI; green/light grey curves: joint effect of RI and price. (c) A molecular analysis may reveal different microstructures of working and engaging in leisure. The three rows show three different hypothetical trials. All three microstructures have the same molar TA, but are clearly distinguishable. (d) Molecular ethogram showing the detailed temporal topography of working and engaging in leisure for the subject in (b). Upper, middle and lower panels show low, medium and high pay-offs, respectively, for a fixed, short price. Following previous reports using rat subjects, releases shorter than 1 s are considered part of the previous work bout (as subjects remain at the lever during this period). Graphically, this makes some work bouts appear longer than the others. The subject mostly pre-commits to working continuously for the entire price duration. When the pay-off is high, the subject works almost continuously for the entire trial, engaging in very short leisure bouts inbetween work bouts. When the pay-off is low, the subject engages in a long leisure bout after receiving a reward. This leisure bout is potentially longer than the trial, whence it would be censored. The part of a trial before the reward, price and probability of reward delivery are certainly known is coloured pink/dark and not considered further. Data collected by Y.-A.B. and R.S. and initially reported in [38]. (Online version in colour.)

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The objective strength of the BSR is the frequency of electrical stimulation pulses applied to the medial forebrain bundle. This is assumed to have a subjective worth, or microscopic utility [18–23] called the reward intensity (RI, in arbitrary units). The transformation from objective to subjective worth has been previously determined [42–47]. The ratio of the RI to the price is called the pay-off. Leisure is assumed to have an intrinsic subjective worth, although its utility remains to be quantified. Throughout a task trial, the objective strength of the reward and price are held fixed. The total time a subject could work per trial is 25 times the price (plus extra time for ‘consuming’ rewards) enabling at most 25 rewards to be harvested. A behaviourally observed work or leisure bout is defined as a temporally continuous act of working or engaging in leisure, respectively. Of course, contiguous short work or leisure bouts are externally indistinguishable from one long bout. Subjects are free to distribute leisure bouts in between individual work bouts.

Subjects face triads of trials: ‘leading’, ‘test’ then ‘trailing’ (electronic supplementary material, figure S1). Leading and

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developed in [18–23]) called the reward intensity (RI, in arbitrary units). The transformation from objective to subjective worth has been previously determined [42–47]. The ratio of the RI to the price is called the pay-off. Leisure is assumed to have an intrinsic subjective worth, although its utility remains to be quantified. Throughout a task trial, the objective strength of the reward and price are held fixed. The total time a subject could work per trial is 25 times the price (plus extra time for ‘consuming’ rewards) enabling at most 25 rewards to be harvested. A behaviourally observed work or leisure bout is defined as a temporally continuous act of working or engaging in leisure, respectively. Of course, contiguous short work or leisure bouts are externally indistinguishable from one long bout. Subjects are free to distribute leisure bouts in between individual work bouts.
Table 1. List of symbols.

<table>
<thead>
<tr>
<th>symbol</th>
<th>meaning</th>
</tr>
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<tbody>
<tr>
<td>$1/\lambda$</td>
<td>mean of exponential effective prior probability density for leisure time</td>
</tr>
<tr>
<td>$\alpha \in [0,1]$</td>
<td>weight on linear component of microscopic benefit-of-leisure</td>
</tr>
<tr>
<td>$\beta \in [0,\infty)$</td>
<td>inverse temperature or degree of stochasticity–determinism parameter</td>
</tr>
<tr>
<td>$\text{CHT}$</td>
<td>cumulative handling time</td>
</tr>
<tr>
<td>$C(t)$</td>
<td>microscopic benefit-of-leisure</td>
</tr>
<tr>
<td>$C_{\text{max}}$</td>
<td>maximum of sigmoidal microscopic benefit-of-leisure</td>
</tr>
<tr>
<td>$C_{\text{shift}}$</td>
<td>shift of sigmoidal microscopic benefit-of-leisure</td>
</tr>
<tr>
<td>$\delta(t)$</td>
<td>delta/indicator function</td>
</tr>
<tr>
<td>$E_{\pi}$</td>
<td>expected value with respect to policy $\pi$</td>
</tr>
<tr>
<td>$K_{\ell}$</td>
<td>slope of linear microscopic benefit-of-leisure</td>
</tr>
<tr>
<td>$L$</td>
<td>leisure</td>
</tr>
<tr>
<td>$\mu_{a}(\tau_{a})$</td>
<td>effective prior probability density of choosing action $a$ for duration $\tau_{a}$ from state $s$</td>
</tr>
<tr>
<td>$\rho$</td>
<td>price</td>
</tr>
<tr>
<td>$\pi([a, \tau_{a}]</td>
<td>s)$</td>
</tr>
<tr>
<td>$\text{post}$</td>
<td>post-reward</td>
</tr>
<tr>
<td>$\text{pre}$</td>
<td>pre-reward</td>
</tr>
<tr>
<td>$Q(s, [a, \tau_{a}])$</td>
<td>expected return or (differential) $Q$-value of taking action $a$, for duration $\tau_{a}$ from state $s$</td>
</tr>
<tr>
<td>$\rho \tau_{a}$</td>
<td>opportunity cost of time for taking action $a$ for duration $\tau_{a}$</td>
</tr>
<tr>
<td>$\text{RI}$</td>
<td>(subjective) reward intensity</td>
</tr>
<tr>
<td>$\hat{P}$</td>
<td>pay-off</td>
</tr>
<tr>
<td>$s$</td>
<td>state</td>
</tr>
<tr>
<td>$\text{TA}$</td>
<td>time allocation</td>
</tr>
<tr>
<td>$\tau_{i}$</td>
<td>duration of instrumental leisure</td>
</tr>
<tr>
<td>$\tau_{pav}$</td>
<td>Pavlovian component of post-reward leisure</td>
</tr>
<tr>
<td>$\tau_{w}$</td>
<td>duration of work</td>
</tr>
<tr>
<td>$W$</td>
<td>work</td>
</tr>
<tr>
<td>$w \in [0,\hat{P}]$</td>
<td>amount of work time so far executed out of the price</td>
</tr>
<tr>
<td>$V(s)$</td>
<td>expected return or value of state $s$</td>
</tr>
</tbody>
</table>

Trailing trials involve maximal and minimal reward intensities, respectively, and the shortest price (we use the qualifiers ‘short’, ‘long’, etc., to emphasize that the price is an experimenter determined time-period). We analyse the sandwiched test trials, which span a range of prices and reward intensities.

3. Molar and molecular analyses of data

The key molar statistic is the TA, namely the proportion of the available time for working in a test trial that the subject spends pressing the lever. Figure 1b shows example TAs for a typical subject. TA increases with the RI and decreases with the price. Conversely, a molecular analysis, shown in the ethograms (in figure 1c,d), assesses the detailed temporal topography of choice, recording when, and for how long, each act of work or leisure occurred (after the first acquisition of the reward in the trial, i.e. after the ‘pink/dark grey’ lever presses in figure 1d). The TA can be derived from the molecular ethogram data, but not vice versa, because many different molecular patterns (figure 1c) share a single TA.

Qualitative characteristics of the molecular structure of the data (figure 1d) include: (i) at high pay-offs, subjects work almost continuously, engaging in little leisure between work bouts; (ii) at low pay-offs, they engage in leisure all at once, in long bouts after working, rather than distributing the same amount of leisure time into multiple short leisure bouts; (iii) subjects work continuously for the entire price duration, as long as the price is not very long (as shown by an analysis conducted by Y.-A.B., to be published separately) and (iv) the duration of leisure bouts is variable.

4. Micro-semi-Markov decision process model

We consider whether key features of the data in figure 1d might arise from the subject’s making stochastic optimal control choices, i.e. ones that at least approximately maximize the expected return arising from all benefits and costs over entire trials. Following [24], we formulate this computational problem using the reinforcement-learning framework of infinite horizon (Semi) Markov decision processes (SIMDPs) [48,49] (figure 2a). Subjects not only choose which action $a$ to take, i.e. to work ($W$) or engage in leisure ($L$), but also the duration of the action ($\tau_{a}$). They pay an automatic opportunity cost of time: performing an action over a longer period denies the subject the opportunity to take other actions during that period, and thus extirpates any potential benefit from those actions.

As trials are substantially extended, we assume that the subjects do not worry about the time the trial ends, and instead make choices that would (approximately) maximize their average summed microscopic utility per unit time [24]. Nevertheless, for comparison to the data, we still terminate each trial at $25\times$ price, so actions can be censored by the end of the trial, preventing their completion.

4.1. Utility

The utility of the reward is RI. We assume that pressing the lever requires such minimal force that it does not incur any direct effort cost. We assume leisure to be intrinsically beneficial according to a function $C_{t}(\tau)$ of its duration (but formally independent of any other rewards or costs). The simplest such function is linear $C_{t}(\tau) = K_{t}\tau$ (figure 2b(i), blue/dark grey line), which would imply that the net utility can readily appreciate them after minimal experience on a given trial without uncertainty.
of several short leisure bouts would be the same as a single bout of equal total length (figure 2h(ii), blue/dark grey line).

Alternatively, \(C_L(.)\) could be supralinear (figure 2h(i), red/grey curve). For this function, a single long leisure bout would be preferred to an equivalent time spent in several short bouts (figure 2h(ii), red/grey curve). If \(C_L(.)\) saturates, the rate of accrual of benefit-of-leisure \(dC_L(t)/dt\) will peak at an optimal bout duration. We represent this class of functions with a sigmoidal \(C_L(.)\) (red/grey), which is initially supralinear but eventually saturates, and so has a unimodal net benefit per unit time; and a weighted sum of these two (green/light grey). See the electronic supplementary material, equation (S-3) for details. (c) Time \(\tau_{\text{Pav}}\) is the Pavlovian component of leisure, reflecting conditioning to the lever. It is decreasing with RI (here, inversely) and increasing with price (here sigmoidally), so that it decreases with pay-off. (Online version in colour.)

**Figure 2.** Model and leisure functions. (a) The infinite horizon micro-SMDP. States are characterized by whether they are pre- or post-reward. Subjects choose not only whether to work or to engage in leisure, but also for how long to do so. Pre-reward states are further defined by the amount of work time \(w\) that the subject has so far invested. At a pre-reward state \([\text{pre, } w]\), the subject can choose to work \((W)\) for a duration \(\tau_W\) or engage in leisure \((L)\) for a duration \(\tau_L\). Working for \(\tau_W\) transitions the subject to a subsequent pre-reward state \([\text{pre, } w+\tau_W]\) if \(w+\tau_W < P\), and to the post-reward state if \(w+\tau_W \geq P\). Engaging in leisure for \(\tau_L\) transitions the subject to the same state. For working, only transitions to the post-reward state are rewarded, with reward intensity \(RI\). Engaging in leisure for \(\tau_L\) has a benefit \(C_L(\tau_L)\). In the post-reward state, the subject is assumed already to have been at leisure for a time \(\tau_{\text{Pav}}\), which reflects Pavlovian conditioning to the lever. By choosing to engage in instrumental leisure for a duration \(\tau_L\), it gains a microscopic benefit-of-leisure \(C_L(\tau_{\text{Pav}}+\tau_L)\), and then returns to state \([\text{pre, } 0]\) at the start of the cycle whence the process repeats. ([b](ii)): canonical microscopic benefit-of-leisure functions \(C_L(.)\); (ii): the net microscopic benefit-of-leisure per unit time spent in leisure. For simplicity, we considered linear \(C_L(.)\) (blue/dark grey), whose net benefit per unit time is constant, sigmoidal \(C_L(.)\) (red/grey), which is initially supralinear but eventually saturates, and so has a unimodal net benefit per unit time; and a weighted sum of these two (green/light grey). See the electronic supplementary material, equation (S-3) for details. (c) Time \(\tau_{\text{Pav}}\) is the Pavlovian component of leisure, reflecting conditioning to the lever. It is decreasing with RI (here, inversely) and increasing with price (here sigmoidally), so that it decreases with pay-off. (Online version in colour.)

4.2. State space

The state \(s \in S\) in the model contains all the information required to make a decision. This comprises a binary component (‘pre’ or ‘post’), reporting whether or not the subject has just received a reward; and a real-valued component, indicating if not, how much work \(w \in [0, P]\) out of the price \(P\) has been performed. Alternatively, \(P-w\) is how far the subject is from the price.

4.3. Transitions

At state \([\text{pre}, w]\), the subject can choose to work \((W)\) for a duration \(\tau_W\) or engage in leisure \((L)\) for a duration \(\tau_L\). If it chooses the latter, it enjoys a benefit-of-leisure \(C_L(\tau_L)\) for time \(\tau_L\), chosen in the light of \(\tau_{\text{Pav}}\) to optimize the expected return. The Pavlovian component comprises a mandatory pause, which is curtailed by the subject’s reengagement (conditioned-response) with the reward (unconditioned-stimulus)-predicting lever (conditioned-stimulus). As we shall discuss, we postulate a Pavlovian component to account for the detrimental leisure bouts at high pay-offs. We assume \(\tau_{\text{Pav}} = f_{\text{Pav}}(RI, P)\) decreases with pay-off—i.e. increases with price and decreases with RI (figure 2c). The net microscopic benefit-of-leisure is then \(C_L(\tau_L + \tau_{\text{Pav}})\) over a bout of total length \(\tau_L + \tau_{\text{Pav}}\).
\[ \tau_W \text{ that go beyond the price, they cannot physically work for longer than this time, because the lever is retracted as the reward is delivered.} \]

In the post-reward state \( s' = [\text{post}] \), the subject can add instrumental leisure for time \( \tau_l \) to the mandatory Pavlovian leisure \( \tau_W \) discussed above. It receives utility \( C_L(\tau_l + \tau_W) \) over time \( \tau_l + \tau_W \), and then transitions to state \( s' = [\text{pre};0] \). The cycle then repeats.

In all the cases, the subject’s next state in the future \( s' \) depends on its current state \( s \), the action \( a \) and the duration \( \tau_l \) but is independent of all other states, actions and durations in the past, making the model an SMDP. The model is molecular, as it generates the topography of lever depressing and releasing. It is microscopic as it commits to particular durations of performing actions. We therefore refer to it as a micro-SMDP. In the Discussion section, we consider an alternate, nanoscopic variant which makes choices at a finer timescale.

### 4.4. Policy evaluation

A (stochastic) policy \( \pi \) determines the probability of each choice of action and duration. It is assumed to be evaluated according to the average reward rate (see electronic supplementary material, equation (S-1)). In the SMDP, the state cycles between [pre-] and [post]-reward. The average reward rate is the ratio of the expected total microscopic utility accumulated during a cycle to the expected total time that a cycle takes. The former comprises RI from the reward and the expected microscopic utilities of leisure; the latter includes the price \( P \) and the expected duration engaged in leisure.

The total average reward rate is

\[
\rho^* = \frac{\text{RI} + \int_{[\text{post}]} C_L(\tau_l + \tau_W) \, d\tau_l + \int_{[\text{pre};0]} C_L(\tau_l + \tau_W) \, d\tau_l}{\text{RI} + \int_{[\text{post}]} \tau_l + \tau_W \, d\tau_l + \int_{[\text{pre};0]} \tau_l + \tau_W \, d\tau_l} \sum_{\tau_l} C_L(\tau_l + \tau_W) \, d\tau_l.
\]

(4.1)

Here, \( \pi([L, \tau_l]) \) and \( \pi_\tau_l \) are the probabilities of engaging in instrumental leisure \( L \) for time \( \tau_l \) in the post-reward and pre-reward state \([\text{pre};w]\), respectively; \( E_\tau \) is the expectation over those probabilities. \( n_{[\text{pre};w]} \) is the (random) number of times the subject engages in leisure in the pre-reward state \([\text{pre};w]\).

For state \( s = \text{post} \), the action \( a = [L, \tau_l] \) of engaging in leisure for time \( \tau_l \) has differential value \( Q^\pi([\text{post},[L, \tau_l]]) \) (see the electronic supplementary material, equation (S-2)) that includes three terms: (i) the microscopic utility of the leisure, \( C_L(\tau_l + \tau_W) \); (ii) opportunity cost \( -\rho^*(\tau_l + \tau_W) \) for the leisure time (the rate of which is determined by the overall average reward rate) and (iii) the long-run value \( V^\pi([\text{pre};0]) \) of the next state. The value of state \( s \) is defined as

\[
V^\pi(s) = \sum_s \pi([a, \tau_a],[s]) Q^\pi([a, \tau_a],[s]),
\]

averaging over the actions and durations that the policy \( \pi \) specifies at state \( s \). Thus,

\[
Q^\pi([L, \tau_l]) = C_L(\tau_l + \tau_W) - \rho^*(\tau_l + \tau_W) + V^\pi([\text{pre};0]).
\]

(4.2)

Note the clear distinction between the immediate microscopic benefit-of-leisure \( C_L(\tau_l + \tau_W) \) and the net benefit of leisure, given by the overall Q-value.

The value \( Q^\pi([\text{pre};w], [L, \tau_l]) \) of engaging in leisure for \( \tau_l \) in the pre-reward state has the same form, but without the contribution of \( \tau_W \), and with a different subsequent state

\[
Q^\pi([\text{pre};w], [L, \tau_l]) = C_L(\tau_l - \rho^* \tau_l + V^\pi([\text{pre};w])).
\]

(4.3)

Finally, the value \( Q^\pi([\text{post},w], [W, \tau_W]) \) of working for time \( \tau_W \) in the pre-reward state has two components, depending on whether or not the accumulated work time \( w + \tau_W \) is still less than the price (defined using a delta/indicator function as \( \delta(w + \tau_W < P) \)).

\[
Q^\pi([\text{post},w], [W, \tau_W]) = \delta(w + \tau_W < P) - \rho^* \tau_W + V^\pi([\text{post};w + \tau_W]) \delta(w + \tau_W \geq P) (\text{RI} - \rho^*(P - w) + V^\pi(\text{post})).
\]

(4.4)

### 4.5. Policy

We assume the subject’s policy \( \pi \) is stochastic, based on a softmax of the (differential) value of each choice, i.e. favouring actions and durations with greater expected returns. Random behavioural lapses make extremely long leisure or work bouts unlikely; we therefore consider a probability density \( \mu_a(\tau_l) \) of choosing duration \( \tau_l \) (potentially depending on the action \( a \)), which is combined with the softmax like prior and likelihood (see the electronic supplementary material, text S1). We consider an alternative in the Discussion. For leisure bouts, we assume \( \mu_a(\tau_l) = \lambda \exp(-\lambda \tau_l) \) is exponential with mean \( 1/\lambda = 10P \). The prior \( \mu_a(\tau_W) \) for work bouts plays little role, provided its mean is not too short. This makes

\[
\pi([a, \tau_a]|s) = \frac{\exp[\lambda Q^\pi(s, [a, \tau_a])]}{\sum_a \int_{[a]} \exp[\lambda Q^\pi(s, [a', \tau_a])] \mu_a(\tau_a) d\tau_a}.
\]

(4.5)

Subjects will be more likely to choose the action with the greatest Q-value, but have a non-zero probability of choosing a suboptimal action. The parameter \( \beta \in [0, \infty) \) controls the degree of stochasticity in choices. Choices are completely random if \( \beta = 0 \), whereas \( \beta \to \infty \) signifies optimal choices. We use policy iteration [48,49] in order to compute policies that are self-consistent with their Q-values: these are the dynamic equilibria of policy iteration (see the electronic supplementary material, text S1). An alternative would be to compute optimal Q-values and then make stochastic choices based on them; however, this would lead to policies that are inconsistent with their Q-values. We shall show that stochastic, approximately optimal self-consistent choices lead to pre-commitment to working continuously for the entire price duration.

### 5. Micro-semi-Markov decision process policies

We first use the micro-SMDP to study the issue of stochasticity, then consider the three main regimes of behaviour evident in the data in figure 1d: when pay-offs are high (subjects work almost all the time), low (subjects never work) and medium (when they divide their time). Finally, we discuss the molar consequences of the molecular choices made by the SMDP. All throughout, RI and P are adopted from experimental data, while the parameters governing the benefit-of-leisure are the free parameters of interest.

#### 5.1. Stochasticity

To illustrate the issues for the stochasticity of choice, we consider the case of a linear \( C_L(\tau_l + \tau_W) = K_L(\tau_l + \tau_W) \) and
make two further simplifications: the subject does not engage in leisure in the pre-reward state (thus working for the whole price); and $\lambda = 0$, licensing arbitrarily long leisure durations. Then the $Q$-value of leisure is linear in $t_L$, so the leisure duration distribution is exponential (see the electronic supplementary material, text S2). The expected reward rate and mean leisure duration can be derived analytically (see the electronic supplementary material, text S3).

As long as $RI - K_L P > 1/\beta$

$$\rho^* = \frac{\beta (RI + K_L \tau_{av}) - 1}{\beta (P + \tau_{av})}$$

and

$$\mathbb{E}[t_L | \text{post}] = \frac{P + \tau_{av}}{\beta (RI - K_L P) - 1}$$

(5.1)

Otherwise, if $RI - K_L P < 1/\beta$, then $\rho^* \rightarrow K_L$ (figure 3e(ii),b(ii)) and the subject would choose to engage in leisure for the entire trial as $\mathbb{E}[t_L | \text{post}] \rightarrow \infty$ (figure 3e(ii),b(ii)).

Deterministically optimal behaviour requires $\beta \rightarrow \infty$. In that case, provided $RI > K_L P$, the subject would not engage in leisure at all ($\mathbb{E}[t_L | \text{post}] = 0$) but would work the entire trial (interspersed by only Pavlovian leisure $\tau_{av}$) with optimal reward rate $\rho^* = (RI + K_L \tau_{av})/(P + \tau_{av})$ (figure 3e(i),b(i) and a(ii),b(ii), respectively, dashed black lines). However, if $RI < K_L P$, then it would engage in leisure for the entire trial. Thus, TA functions would be step functions of the RI and price, as shown by the dashed black lines in figure 3f(iii),b(iii).

Of course, as is amply apparent in figure 1d, actual behaviour shows substantial variability, motivating stochastic choices, with $\beta < \infty$. As all the other quantities can be scaled, we set $\beta = 1$ without loss of generality. This leads to smoothly changing TA functions, expected leisure durations and reward rates, as shown by the solid lines in figure 3. We now return to the general case ($\lambda \neq 0$, and leisure is possible in the pre-reward state).

5.2. High pay-offs

The pay-off is high when the RI is high or the price is short, or both. Subjects work as much as possible, making the reward rate in equation (4.1) $\rho^* = (RI + C_t(\tau_{av}))/P + \tau_{av})$. As $\tau_{av}$ is small for high pay-offs, $\rho^* \approx RI/P$ is just the pay-off of the trial. The opportunity cost of leisure time $\rho^*(t_L + \tau_{av})$ is then linear with a very steep slope (dash-dotted line in figure 4d(i)), which dominates $C_t(\tau_{av} + \tau_{av})$ (dashed line in figure 4d(ii)), irrespective of which form it follows. The $Q$-value of engaging in leisure in the post-reward state then becomes the linear opportunity cost of leisure time, i.e. $Q^*(\text{post}, t_L, \tau_L) \rightarrow -\rho^*(t_L + \tau_{av})$ (solid bold line in figure 4d(ii)).

From equation (4.5), the probability density of engaging in instrumental leisure for time $t_L$ is $\pi(t_L, \tau_{post}) \propto \exp[-(\beta \rho^* + \lambda) t_L]$. This is an exponential distribution with very short mean $1/\beta \rho^* + \lambda$ (figure 4d(ii)). The net post-reward leisure bout, consisting of both Pavlovian and instrumental components has the same distribution, only shifted by $\tau_{av}$, i.e. a lagged exponential distribution with mean $\tau_{av} + 1/\beta \rho^* + \lambda$ (figure 4f).

The probability of choosing to engage in leisure in a pre-reward state (i.e. after the potential resumption of working) is correspondingly also extremely small. Furthermore, the steep opportunity cost of not working would make the distribution of any pre-reward leisure duration also be approximately a very short mean exponential (but not lagged by $\tau_{av}$, figure 4b,c). Therefore when choosing to work, the duration of the work bout chosen ($\tau_{av}$) barely matters (as revealed by the identical $Q$-values and policies for different work bout durations in figure 4d,e). That is, irrespective of which the subject performs numerous short work bouts or pre-commits to working the whole price, it enjoys the same expected return. To the experimenter, the subject appears to work without interruption for the entire price. In summary, for high pay-offs, the subject works almost continuously, with very short, lagged-exponentially distributed leisure bouts at the end of each work bout (figure 5b, lowest panel). This accounts well for key feature (i) of the data.

5.3. Low pay-offs

At the other extreme, after discovering that the pay-off is very low, subjects barely work (figure 1d(ii)). Temporarily ignoring leisure consumed in the pre-reward state, the reward rate in equation (4.1) becomes

$$\rho^* \approx \frac{\mathbb{E}[\text{post}, t_L] | \text{post} | C_t(\tau_{av} + \tau_L)}{P + \mathbb{E}[\text{post}, t_L] | \text{post} | \tau_{av} + \tau_L},$$

as shown by the dash-dotted line in figure 6(i), and is comparatively small. The opportunity cost of time grows so slowly that the $Q$-value of leisure is dominated by the microscopic benefit-of-leisure $C_t(\tau_{av} + \tau_L)$ (dashed curves in figure 6(i)).

We showed that for linear $C_t(\cdot)$, the $Q$-value is linear and the leisure duration distribution is exponential (shown again in figure 6a, left panel). For initially supralinear $C_t(\cdot)$, the $Q$-value becomes a bump (solid bold curve in figure 6a(i), centre and right). The probability of choosing to engage in instrumental leisure for time $t_L$ is then the exponential of this bump, which yields a unimodal, gamma-like distribution (figure 6a(ii), centre and right). Thus for a low pay-off, a subject would opt to consume leisure all at once go, if from the mode of this distribution. This accounts for key feature (ii) of the data.
The net duration of leisure in the post-reward state \( \tau_L + \tau_{PW} \) is then almost the same unimodal gamma-like distribution (figure 6f). If the Pavlovian component is increased, the instrumental component \( \pi(\tau_L|\text{post}) \) will decrease leaving identical the distribution of their sum \( Pr(\tau_L + \tau_{PW}|\text{post}) \) (cf. figure 6a(ii), right panel).

The location of the mode of the net leisure bout duration distribution (figure 6f) is crucial. For shorter prices associated with low net pay-offs, this mode lies much beyond the trial duration \( T = 25P \). Hence, a leisure bout drawn from this distribution would almost always exceed the trial duration, and so be censored, i.e. terminated by the end of the trial. Our model successfully predicts the molecular data in this condition (figure 5a, upper panel). We discuss our model’s predictions for long prices later.

The main effect of changing from partially linear to saturating \( C_L(\cdot) \) is to decrease both the mean and the standard deviation of leisure bouts. The tail of the distribution (figure 6a, centre versus right panel) is shortened, because the \( Q \)-values of longer leisure bouts ultimately fail to grow.

Engaging in leisure in post- and pre-reward states are closely related. Thus, if the pay-off is too low then the subject will also choose to engage in long leisure bouts in the pre-reward state (figure 6b,c). Correspondingly, the subject will be less likely to commit to longer work times and lose the benefits of leisure (figure 6d,e). If behaviour is too deterministic, then the behavioural cycle from pre- to post-reward can fail to complete (leading to non-ergodicity). This is not apparent in the behavioural data, so we do not consider it further.
5.4. Medium pay-offs

The opportunity costs of time for intermediate pay-offs are also intermediate. Thus, the $Q$-value of leisure (solid bold curves in figure 7(a(i))) depends delicately on the balance between the benefit-of-leisure and the opportunity cost (dashed and dashed-dotted lines in figure 7(a(i)), respectively). For the sigmoidal $C_L(\cdot)$, the combination of supra- and sublinearity leads to a bimodal distribution for leisure bouts that is a weighted sum of an exponential and a gamma-like distribution (figure 7(a(ii)), centre and right panels; f).

Bouts drawn from the exponential component will be short. However, the mode of the gamma-like distribution lies beyond the trial duration (figure 7(f)), as in the low pay-off case when the price is not long (figure 6(f)). Bouts drawn from this will thus be censored. Altogether, this predicts a pattern of several work bouts interrupted by short leisure bouts, followed by a long, censored leisure bout (figure 5a, middle panel). Occasionally, a long, but uncensored, duration can be drawn from the distribution in figure 7(f). The subject would then engage in a long, uncensored leisure bout before returning to work. Our model thus also accounts well for the details of the molecular data on medium pay-offs, including variable leisure bouts (key feature (iv)).

5.5. Pre-commitment to working continuously for the entire price duration

The micro-SMDP model accounts for feature (iii) of the data that subjects generally work continuously for the entire price duration. That is, subjects could choose to pre-commit by working for the entire price $P$, or divide $P$ into multiple contiguous work bouts. In the latter case, even if $Q$-value of working is greater than that of engaging in leisure, the stochasticity of choice implies that subjects would have some chance of engaging in leisure instead, i.e. the pessimal choice (figure 7(b,c)). Pre-committing to working continuously for the entire price avoids this corruption (figure 7(d,e)). In figure 7(c), for any given state [pre, $w$] the probability of choosing longer work bouts $\tau_W$ increases, until the price is reached. Corruption does not occur for a deterministic, optimal policy, so pre-commitment is unnecessary. This case is then similar to that for a high pay-off (figure 4(d,e)).

5.6. Molar behaviour from the micro-semi-Markov decision process

If the micro-SMDP model accounts for the molecular data, integrating its output should account for the molar characterizations of behaviour that were the target of most previous modelling. Consider first the case of a fixed short price $P = 4s$, across different reward intensities (figure 8a). After an initial region in which different $C_L(\cdot)$ affect the outcome, the reward rate $\rho^p$ in equation (4.1) increases linearly with the RI (figure 8a(i), left panel). Consequently, the opportunity cost of time increases linearly too. If $C_L(\cdot)$ is linear, the resultant linear $Q$-value of leisure in the post-reward state, and hence, the mean of the exponential leisure bout duration distribution decreases (figure 8a(ii) and a(iii), centre panels, respectively). If $C_L(\cdot)$ is sigmoidal, the bump corresponding to the $Q$-value of leisure shifts leftwards to smaller leisure durations (figure 8a(i), right panel). Both the mode and the relative weight of the gamma-like distribution decrease as the RI increases (figure 8a(i), right panel). Thus, as the model smoothly transitions from low through medium-to-high reward intensities, TA increases smoothly from zero to one (figure 8a(ii), left panel).

The converse holds if the price is lengthened while holding the RI fixed at a high value, making the TA decrease smoothly (figure 8b(ii)). The reward rate $\rho^p$ in equation (4.1) decreases hyperbolically, eventually reaching an asymptote (at a level depending on $C_L(\cdot)$, figure 8b(i), left panel). For

Figure 5. Micro-SMDP model with stochastic, approximately optimal choices accounts for key features of the molecular data. Ethogram data from left: experiment and right: micro-SMDP model. Upper, middle and lower panels show low, medium and high pay-offs, respectively. Pink/dark bars show work bouts before the subject knows what the reward and price are. These are excluded from all analyses, and so do not appear on the model plot. (Online version in colour.)
long prices, the mode of the unimodal distribution does not increase by much as the price becomes longer. However, by design of the experiment, the trial duration increases with the price. When the trial is much shorter than this mode, most long leisure bouts are censored and TA is near zero. As the trial duration approaches the mode, long leisure bouts are less likely to get censored (figure 8c, left panel).

We therefore make the counterintuitive prediction that as the price becomes longer, subjects will eventually be observed to resume working after a long leisure bout. Thus with longer prices, proportionally more work bouts will be observed (figure 8c, right panel). Consequently, TA would be observed to not decrease, and even increase with the price (see the foot of the red/grey curve in figure 8b(ii), left panel). Such behaviour would be observed for eventually sublinear benefits-of-leisure. An increase in TA at long prices is not possible for linear C_L(.) (blue/dark grey curve in figure 8b(ii), left panel). As the price becomes longer, so does the mean of the resultant exponential leisure bout duration distribution (figure 8b, centre panels) and long leisure bouts will still be censored.

In general, for the same RI and price, less time is spent working for linear than saturating C_L(.) (compare the blue/dark grey and red/grey curves figure 8a(ii),b(ii), left panels), because linear C_L(.) is associated with longer leisure bouts. Thus, larger pay-offs are necessary to capture the entire range of TA. The effect of different C_L(.) on the reward rate at low pay-offs is more subtle (compare blue/dark grey and red/grey curves in figure 8a(i),b(i), left panels). This depends on the ratio of the expected microscopic benefit-of-leisure \( E[p(L_t - \tau_l)] C_L(\tau_{Pav} + \tau_l) \) and the expected leisure duration \( E[p(L_t - \tau_l)] \tau_l + \tau_{Pav} \) in the reward rate equation (equation (4.1)). This is constant (=K_L) for a linear C_L(.). The latter term can be much greater for a saturating C_L(.), leading to a lower reward rate.

Figure 8 shows that the Pavlovian component of leisure \( \tau_{Pav} \) will mainly be evident at shorter prices. At high reward intensities, instrumental leisure is negligible and
leisure is mainly Pavlovian. That TA for real subjects saturates at 1, implies that $Pav$ decreases with pay-off, as argued.

6. Discussion

Real-time decision-making involves choices about when and for how long to execute actions as well as which to perform. We studied a simplified version of this problem, considering a paradigmatic case with economic, psychological, ethological and biological consequences, namely working for explicit external rewards versus engaging in leisure for its own implicit benefit. We offered a normative, microscopic framework accounting for subjects’ temporal choices, showing the rich collection of effects associated with the way that the subjective benefit-of-leisure grows with its duration. Our microscopic formulation involved an infinite horizon SMDP with three key characteristics: approximate optimization of the reward rate, stochastic choices as a function of the values of the options concerned and an assumption that, $a$ priori, temporal choices would never be infinitely extended (owing to either lapses or the greater uncertainty that accompanies the timing of longer intervals [55]). The metrics associated with this last assumption had little effect on the output of the model. We may have alternately assumed that arbitrarily long durations could be chosen as frequently as short ones but more noisily executed; we imputed all such noise to the choice rule for simplicity.

We exercised our model by examining a psychophysical paradigm called the CHT schedule involving BSR. The CHT controls both the (average) minimum inter-reward interval and the amount of work required to earn a reward. More common schedules of reinforcement, such as fixed ratio, or variable interval, control one but not the other. This makes the CHT particularly useful for studying the choice of how long to either work or engage in leisure. Nevertheless, it would be straightforward to adapt our model to treat waiting schedules, such as [56–62] or to add other

![Figure 7.](a–f) $Q$-values and policies for a medium pay-off. Panel positions as in figure 4. RI = 1.76, price $P = 4s$. (Online version in colour.)
facets. For instance, effort costs would lead to shorter work bouts rather than the pre-commitment to working for the duration of the price observed in the data. Costs of waiting through a delay would also lead subjects to quit waiting earlier than later. Other tasks with other work requirements could also be fitted into the model by changing the state and transition structure of the Markov chain. The main issue the CHT task poses for the model is that it is separated into episodic trials of different types making infinite horizon optimization an approximation. However, the approximation
is likely benign, because the relevant trials are extended (each lasts 25 times the price), and the main effect is that work and leisure bouts can sometimes be censored at the ends of trials.

It is straightforward to account for subjects’ behaviour in the CHT when pay-offs are high (i.e. when the rewards are big and the price is short and the subjects work almost all the time) or low (vice versa, when the subjects barely work at all). The medium pay-off case involves a mixture of working and leisure and is more challenging. As the behaviour of the model is driven by relative utilities, the key quantity controlling the allocation of time is the microscopic benefit-of-leisure function. This qualitatively fits the medium pay-off case when it is sigmoidal. Then, the predicted leisure duration distribution is a mixture of an exponential and a gamma-like component, with the weight on the longer, gamma-like component decreasing with pay-off.

The microscopic benefit-of-leisure function reflects a subject’s innate preference for the duration of leisure when only considering leisure. It is independent of the effects of all other rewards and costs. It is not the same as the Q-value of leisure, which is pay-off dependent because it includes the opportunity cost of time (see equation (4.2)). For intuition about the consequences of different functions, consider the case of choosing between taking a long holiday all at one go, or taking multiple short holidays of the same net duration. Given a linear microscopic benefit-of-leisure function, these would be equally preferred; however, sigmoidal functions (or other functions with initially supralinear forms) would prefer the former. A possible alternate form for the benefit-of-leisure could involve only its maximum utility or the utility at the end of a bout [63]; however, the systematic temporal distribution of leisure in the data suggest that it is its duration which is important.

Stochasticity in choices had a further unexpected effect in tending to make subjects pre-commit to a single long work bout rather than dividing work up into multiple short bouts following on from each other. The more bouts the subject used for a single overall work duration, the more probably stochasticity would lead to a choice in favour of leisure, and thus the lower the overall reward rate. Pre-commitment to a single long duration avoids this. Our model therefore provides a novel reason for pre-commitment to executing a choice to completion: the avoidance of corruption owing to stochasticity. If there was also a cost to making a decision—either from the effort expended or from starting and stopping the action at the beginning and ends of bouts, then this effect would be further enhanced. Such switch costs would mainly influence pre-commitment during working rather than the duration of leisure, because there is explicitly one behavioural switch in the latter no matter how long it lasts.

Even at very high pay-offs, subjects are observed still to engage in short leisure bouts after receiving a reward—the so-called post-reinforcement pause (PRP). This is apparently not instrumentally appropriate, and so we consider PRPs to be Pavlovian. The PRP may consist of an obligatory initial component, which is curtailed by the subject’s Pavlovian response to the lever. This obligatory component could be owing to the enjoyment or ‘consumption’ of the reward. The task was set up so that instrumental rather than Pavlovian components of leisure dominate, so for simplicity we assumed the latter to be a pay-off-dependent constant (rather than being a random variable). We can only model PRPs rather crudely, given the paucity of independent data to fit—but our main conclusions are only very weakly sensitive to changes.

By integrating molecular choices we derived molar quantities. A standard molar psychological account assumes that subjects match their TA between work and leisure to the ratio of their pay-offs as in a form of the generalized matching law [8,9,11,14,16]. This has been used to yield a three-dimensional relationship known as a mountain, which directly relates TA to objective reward strength and price [19,21]. However, the algorithmic mountain models depend on a rather simple assignment of utility to leisure that does not have the parametric flexibility to encompass the issues on which our molecular model has focussed. Those issues can nevertheless have molar signatures—for instance, if the microscopic benefit-of-leisure is eventually sublinear, then as the price becomes very long, extended leisure bouts are less likely to be censored, and so the subject would then be observed to resume working before the end of the trial. Integrating this, at long prices, TA would be observed not to decrease, and even increase with the price, a prediction not made by any existing macroscopic model. Whereas animals have been previously shown to consistently work more when work requirements are greater (e.g. ostensibly owing to sunk costs [64]), the apparent anomaly discussed here only occurs at very long prices and is unexpected from a macroscopic perspective. Our microscopic model predicts how this anomaly can be resolved. Experimentally testing whether this prediction holds true would shed light on the types of nonlinear microscopic benefit-of-leisure functions and their parameters actually used by subjects.

Another standard molar (but computational) approach comes from the microeconomic theory of labour supply [1]. Subjects are assumed to maximize their macroscopic utility over combinations of work and leisure [3,5,18]. If work and leisure were imperfect substitutes, so leisure is more valuable given that a certain amount of work has been performed, and/or vice versa, then perfect maximizers would choose some of each. Such macroscopic utilities do not distinguish whether leisure is more beneficial because of recent work, e.g. owing to fatigue. We propose a novel microscopic benefit-of-leisure, which is independent of the recent history of work. We use stochasticity to capture the substantial variability evident at a molecular scale, and thus also molar TA.

Behavioural economists have investigated real-life TA [2,3,5], including making predictions which seemingly contradict those made by labour supply theory accounts [4]. For instance, Camerer et al. [4] found that New York City taxi drivers gave up working for the day once they attained a target income, even when customers were in abundance. Contrary to this finding, in the experimental data we model, subjects work nearly continuously when the pay-off is high rather than giving up early. Income-targeting could be used when the income earned from work can be saved, and then spent on essential commodities and leisure activities [65]. Once sufficient quantities of the latter can be guaranteed, there is no need to earn further income from work. In the experimental data, we model a reward-like BSR cannot be saved for future expenditures, a possible reason why we do not see income-targeting effects.

One class of models that does make predictions at molecular as well as molar levels involves the continuous time Markov chains popular in ethology [17]. In these models, the entire stream of observed behaviour (work and leisure bouts) can be summarized by a small set of parametric distributions, and the effect of variables, for example pay-off,
can be assessed with respect to how those parameters change. These models are descriptive, characterizing what the animal does, rather than being normative: positing why it does so.

Our micro-SMDP model has three revealing variants. One is a nanoscopic MDP, for which choices are made at the finest possible temporal granularity rather than having determinable durations (so a long work bout would turn into a long sequence of ‘work-work-work . . . ’ choices). This model has a straightforward formal relationship to the micro-SMDP model [66]. The distinction between these formulations cannot be made behaviourally, but may be possible in terms of their neural implementations. The second, minor alteration, restricts transitions to those between work and leisure, precluding the above long sequences of choices. The third variant is to allow a wider choice of actions, notably a ‘quit’, which would force the subject to remain at leisure until the end of the trial. This is simpler and can offer a normative account of behaviour for high and low pay-offs. However, in various cases, subjects resume working after long leisure bouts, whereas this should formally not be possible following quitting.

Considered more generally, quitting can be seen as an extreme example of correlation between successive leisure durations—and it is certainly possible that quantitative analyses of the data will reveal subtler dependencies. One source of these could be fatigue (or varying levels of attention or engagement). The CHT procedure (with trailing trials enabling sufficient rest) was optimized to provide stable behavioural performance over long periods. However, fatigue together with the effect of pay-off might explain aspects of the microstructure of the data, especially on medium pay-off trials. Fatigue would lead to runs of work bouts interspersed with short leisure bouts, followed by a long leisure bout to reset or diminish the degree of fatigue. Note, however, that fatigue would make the benefit-of-leisure depend on the recent history of work.

We modelled epochs in a trial after the RI and price are known for sure. The subjects repeatedly experience the RI and price conditions during training over many months, and so would be able to appreciate them after minimal experience on a given trial. However, before this minimal experience, subjects face partial observability, and have to decide whether to explore (by depressing the lever to find out about the benefits of working) or exploit the option of leisure (albeit in ignorance of the price). This leads to a form of optimal stopping problem. However, the experimental regime is chosen broadly so that subjects almost always explore to get at least one sample of the reward and the price (the pink/dark grey shaded bouts in figure 1d).

Finally, having raised computational and algorithmic issues, we should consider aspects of the neural implementation of the microscopic behaviour. The neuromodulator dopamine is of particular interest. Previous macroscopic analyses from pharmacological and drugs of addiction studies have revealed that an increase in the tonic release of the neuromodulator dopamine shifts the three-dimensional relationships towards longer prices [21–23], as if, for instance, dopamine multiplies the intensity of the reward. Equally, models of instrumental vigour have posited that tonic dopamine signals the average reward rate, thus realizing the opportunity cost of time [24,67,68]. This would reduce the propensity to be at leisure. It has also suggested to affect Pavlovian conditioning [69,70] to the reward-delivering lever. Except at very high pay-offs, in our model this by itself would have minimal effect, because instrumental leisure durations would be adjusted accordingly. Finally, it has been suggested as being involved in overcoming the cost of effort [71], a factor that could readily be incorporated into the model. While the ability to discriminate between these various factors is lost in macroscopic analyses, we hope that a microscopic analysis will distinguish them.

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